



Applications of soliton interactions in rogue wave theory and in understanding the impact of vessel wakes

(Learning from dynamics working for and against us)

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1918

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Instead of Introduction: some words from classical authors

There are three states in
a human's life:

alive

dead

on sea



Anacharsis,
Scythian philosopher, VI century B.C.

Strabo makes him the (probably legendary)
inventor of the anchor with two flukes



Outline

- Extremes in wave fields and single waves
- Ship waves in shallow water: threat and treasure
- Monster waves – dangerous sisters of ship waves?
- Jet currents – triggers of monster waves?
- Reaction of coasts to “new” waves



Extremes on the sea

or how “extreme” could be
an extreme (wave) event



Baltic Sea

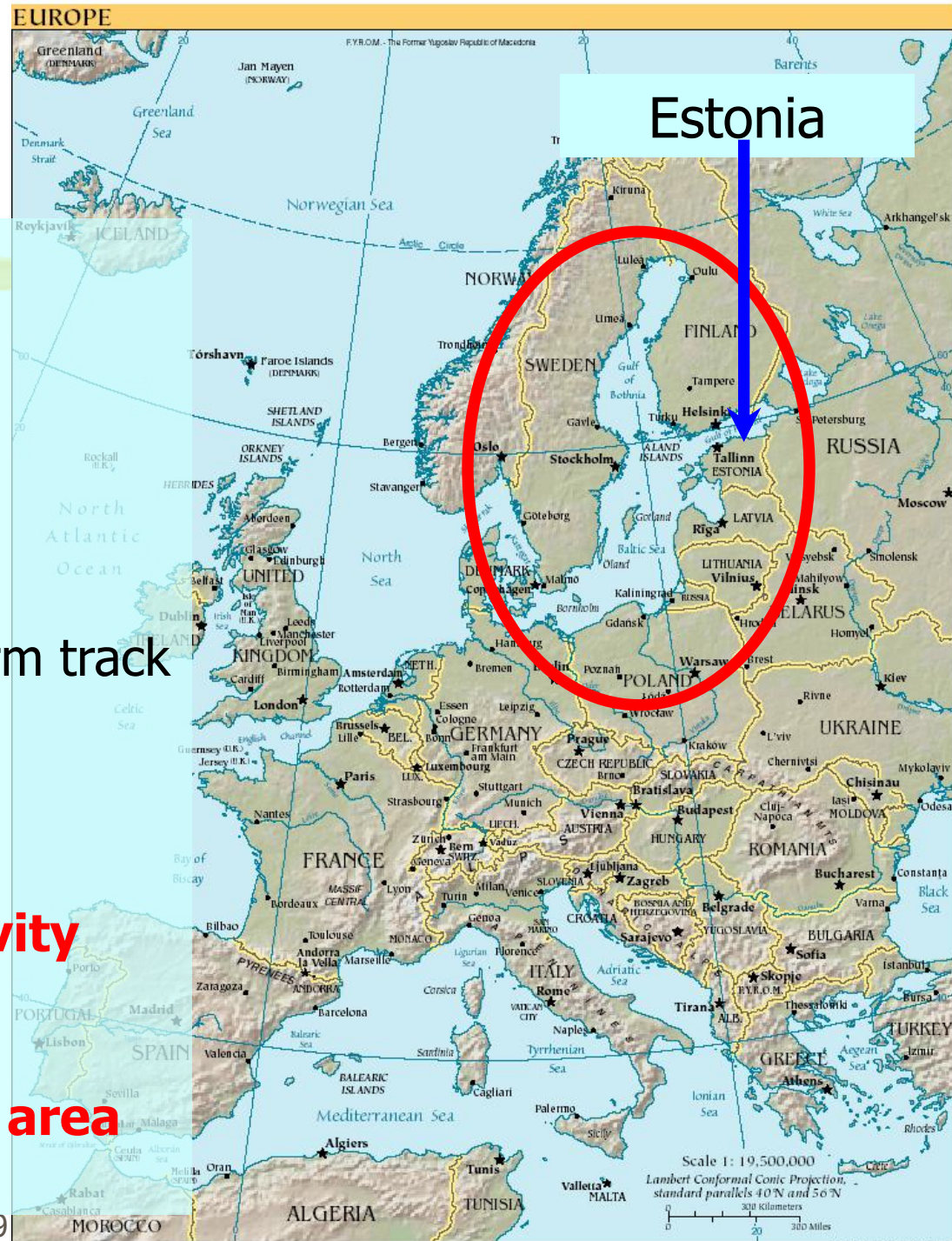
380,000km²

- Long coastline
- no tides
- no jet currents
- short fetch
- low winds, small cyclones
- located on the Atlantic storm track
- brackish water
- variety of different shores
- postglacial uplift

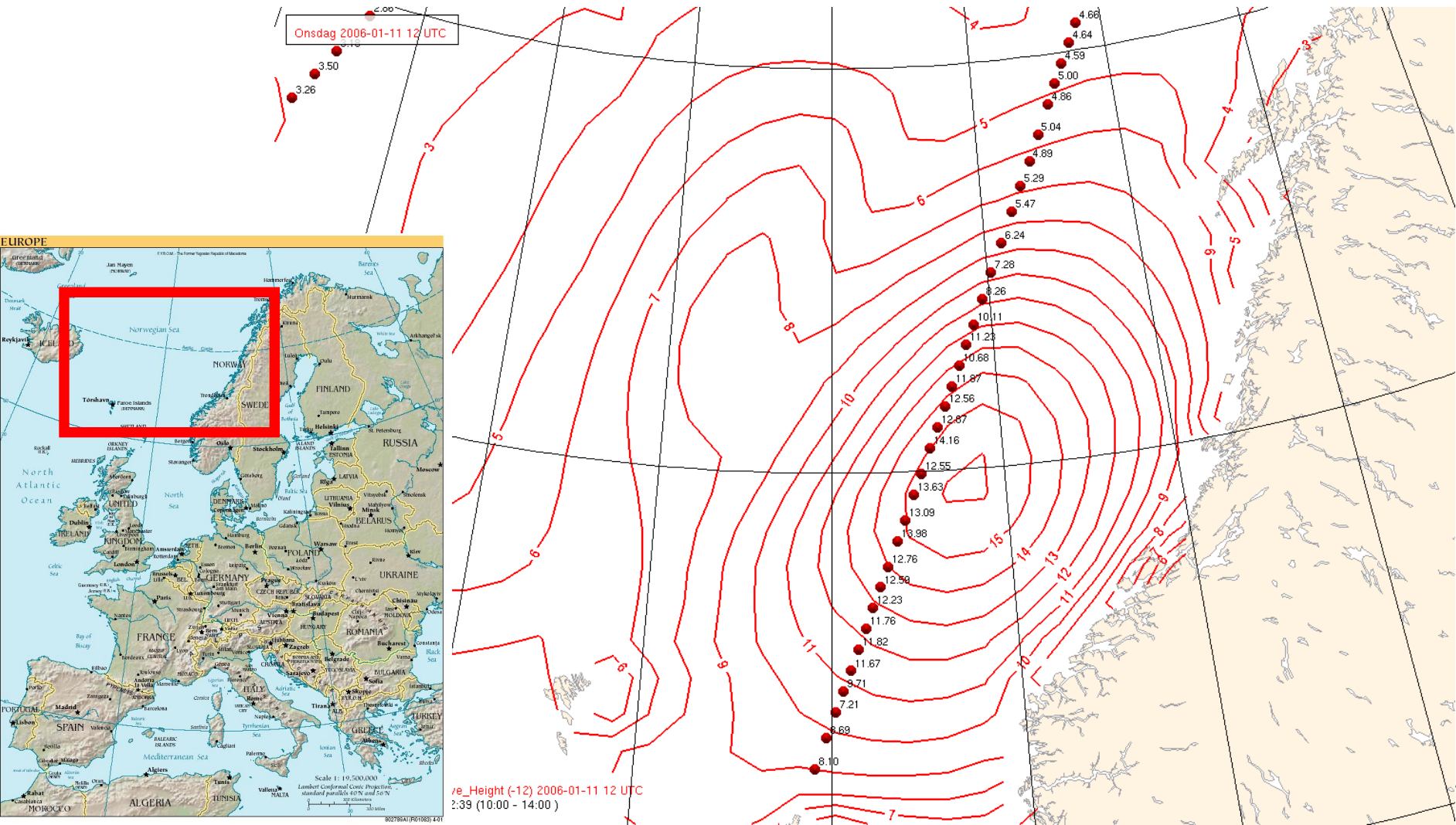
→ low hydrodynamic activity

→ extremely vulnerable

particularly sensitive sea area
by IMO



Feb 2000 & Jan 2006: ever highest waves in North Atlantic





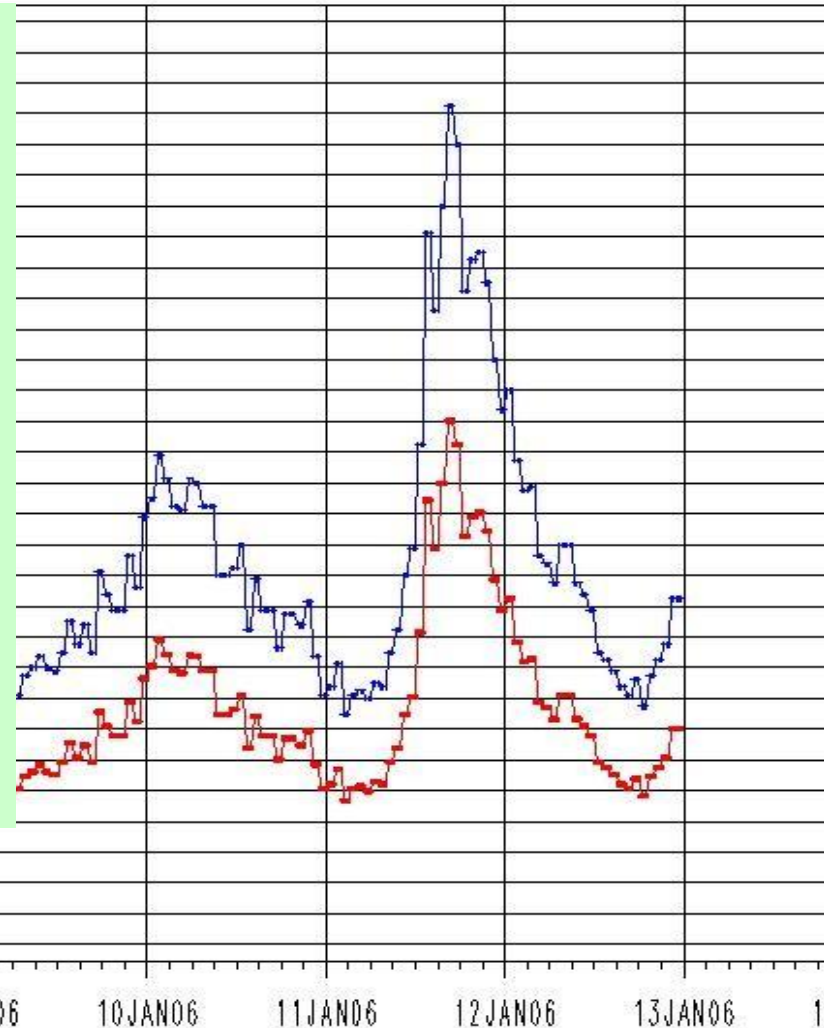
Significant wave height >17 m single waves >27 m

Claims for highest H_s :

17.9 m (Ivan, 15.09.2004, Gulf of Mexico, single wave 27.7m, Wang et al., *Science*, August 2005)

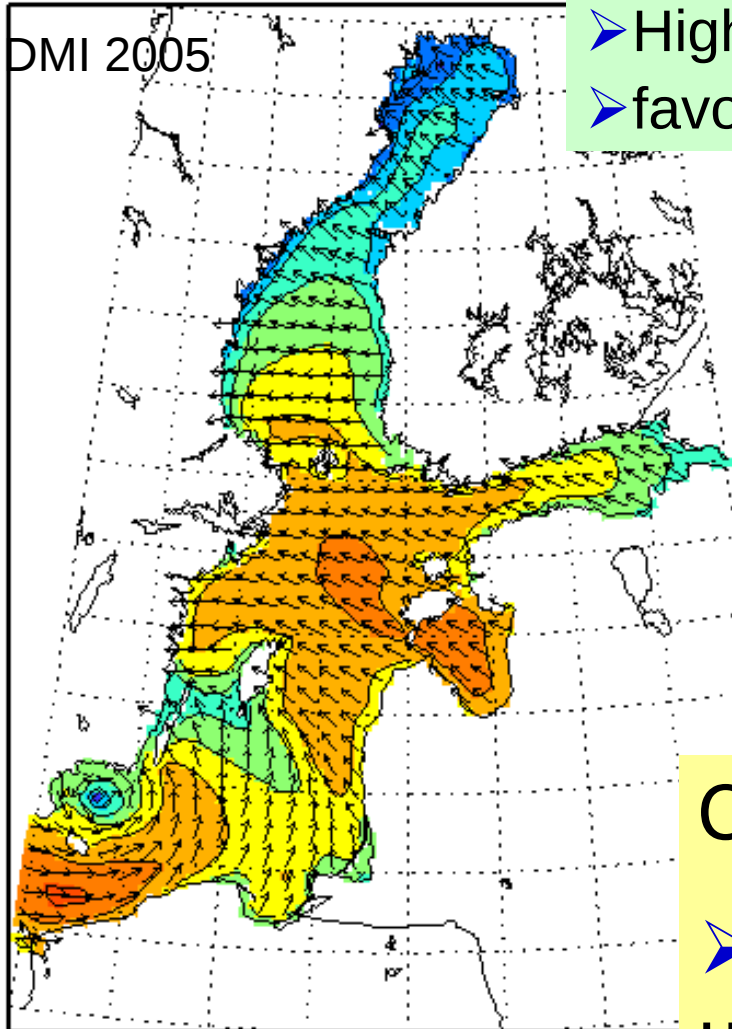
18.5m (Rockall, west of Scotland, Feb.2000; Holliday et al., *GRL* 2006)

Single wave 32.3m: Typhoon Krosa, 06.10.2007 (Liu et al., *Ann. Geophys.*, 2008)



Typical Baltic Sea storms:

wind direction frequently varies within even one subbasin



- High-latitude cyclones are relatively small,
- favourable conditions for large waves seldom

**High & long waves
may only occur if:**

- (i) strong wind
- (ii) blows steadily
- (iii) over large sea area
- (iv) long time

Consequence for the Baltic Sea:

- wave heights and periods usually moderate

Sign. wave height

Waves in the Baltic Sea:

$H_s > 7\text{m}$ happens 1-2 times/decade;
All-time maximum $H_s = 7.82\text{ m}$ (1984)

5.2 m
15.11.2001

7.82 m
1984

7.7 m
23.12.2004

- January 1984: $H_s = 7.82\text{ m}$
- (strong storm in January 1993)
- December 1999: twice $H_s > 7\text{m}$
- 23 Dec 2004: $H_s = 7.7\text{ m}$
- 09 Jan 2005: $H_s = 7.2\text{ m}$

10 m ?! for
09.01.2005

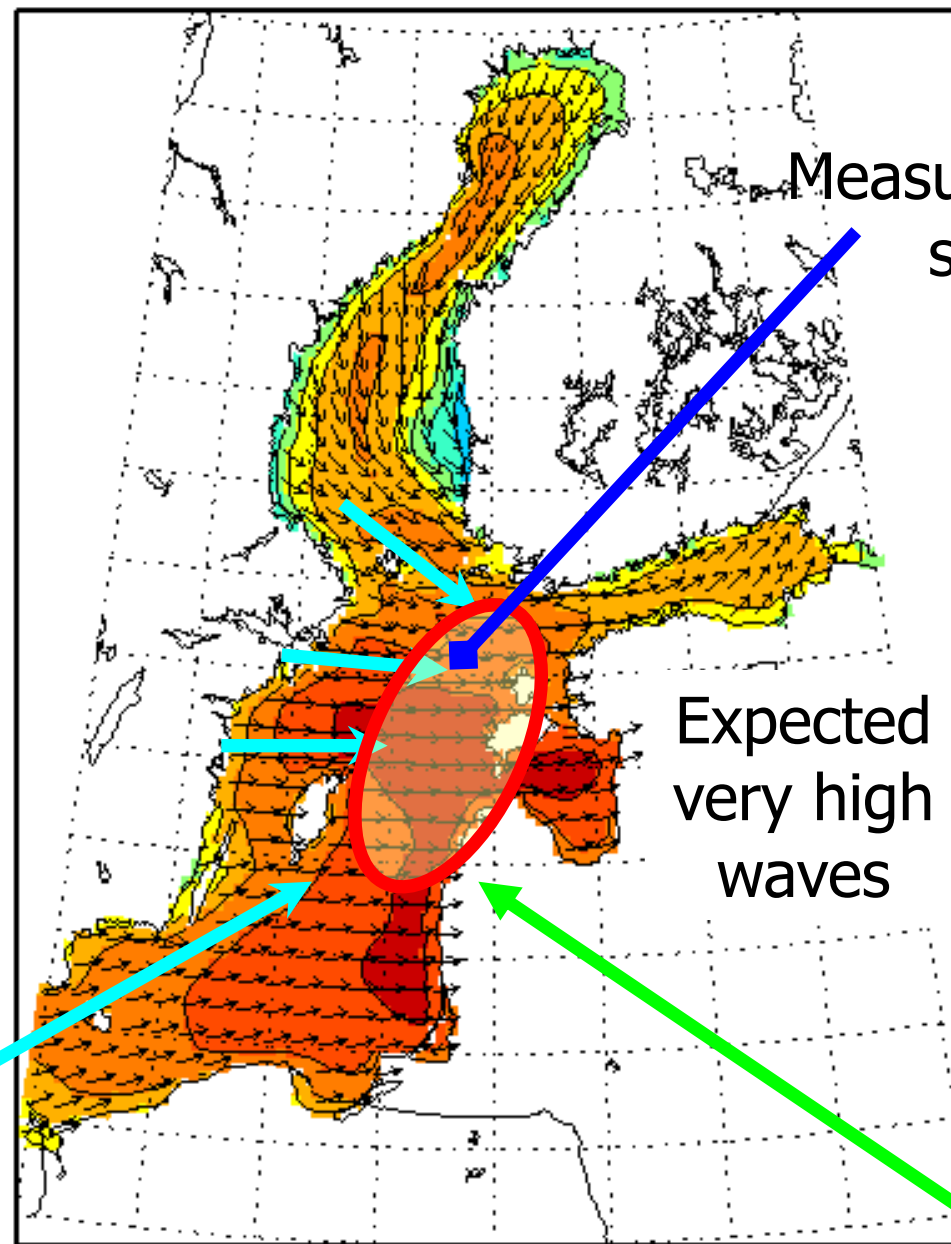
Thus the experts believed that
 $H_s \sim 8\text{--}8.5\text{ m}$ cannot be exceeded

Wind at 10m (m/s): 2005 JAN 09 at 06z

January 2005:
probably the
roughest wave
conditions in
the history

Partially
caused by
convergent
wind pattern

(DMI forecast
released at 06:00
GMT 7.01.2005)



Measurement
site

Expected
very high
waves

Look at wind convergence pattern and imagine wave propagation!!!

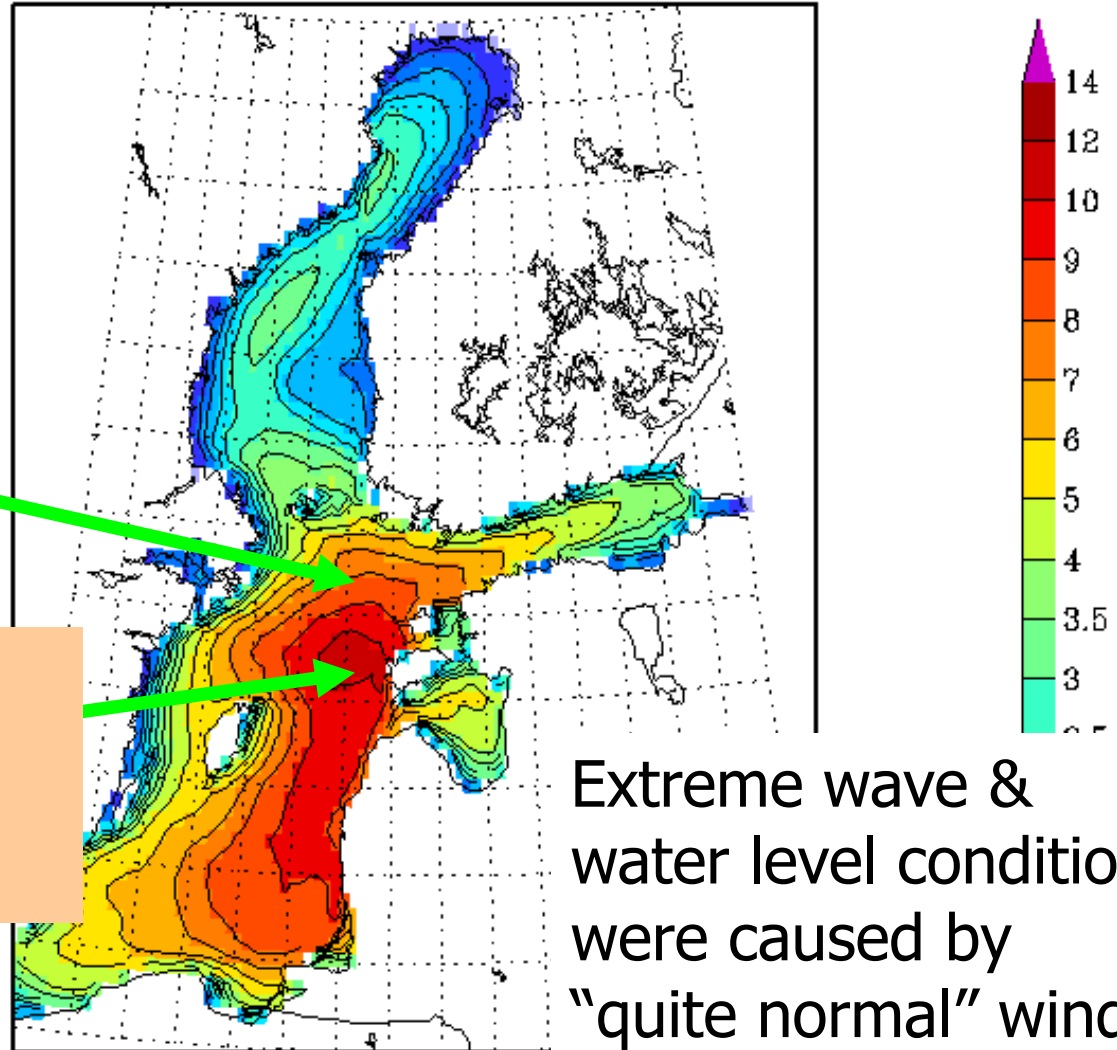
Sign. wave height: 2005 jan 09 06z

The maximum
wave height this
night?

Measured 7.2 m;
model 8.5 m

Model >11m;

Hindcast H_s : ~9.5 m
(+22% !)



Extreme wave &
water level conditions
were caused by
“quite normal” winds
(<29 m/s)

Soomere, Behrens, Tuomi & Nielsen,
Natural Hazards and Earth System Sciences, 2008.

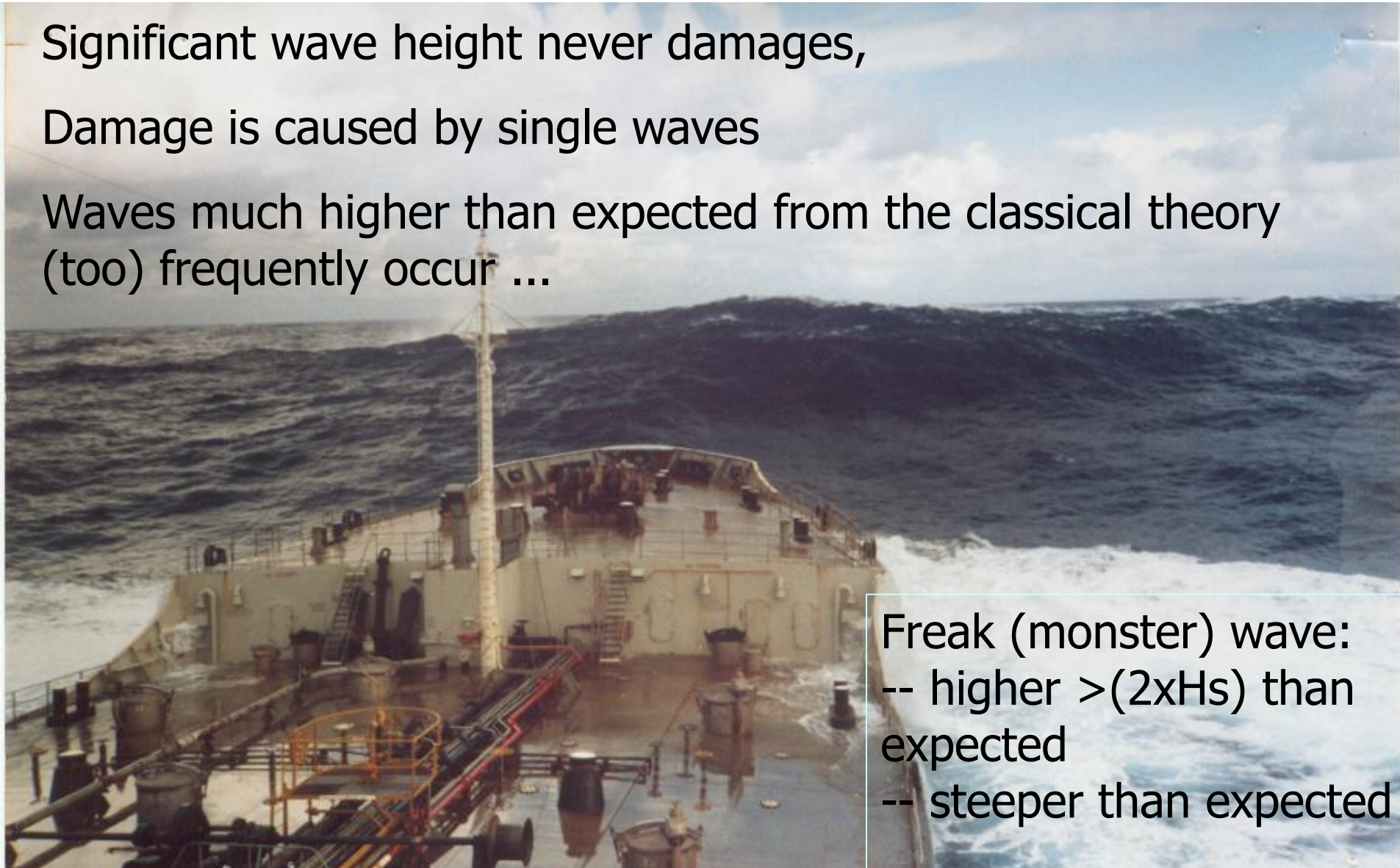


Dynamic extremes: monster waves

Significant wave height never damages,

Damage is caused by single waves

Waves much higher than expected from the classical theory
(too) frequently occur ...



Freak (monster) wave:
-- higher $>(2xH_s)$ than expected
-- steeper than expected



... and frequently
causing heavy damage

... or coming from
unexpected direction

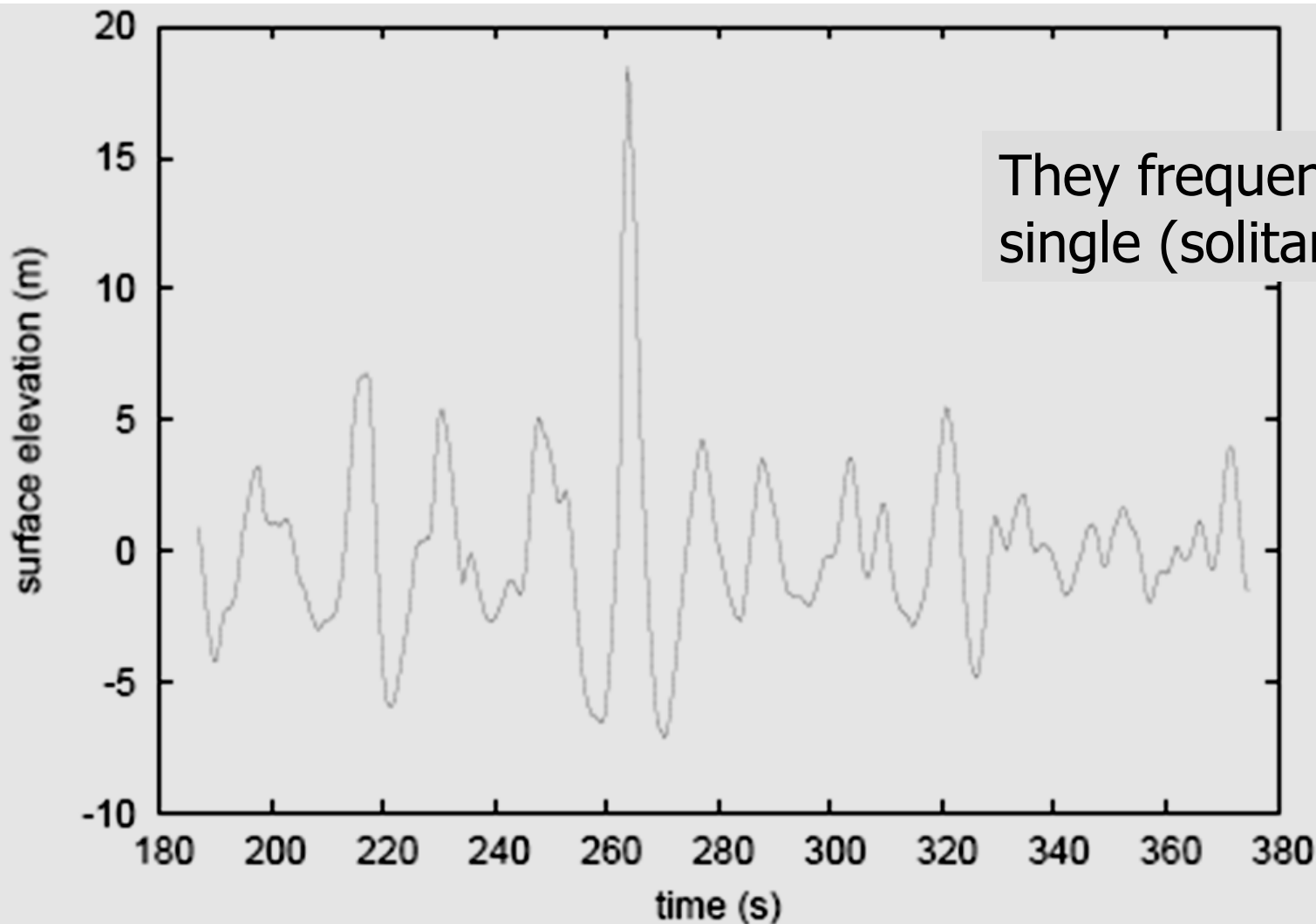




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They do exist in the ocean: Draupner platform, 01 January 1995



They frequently are
single (solitary) waves

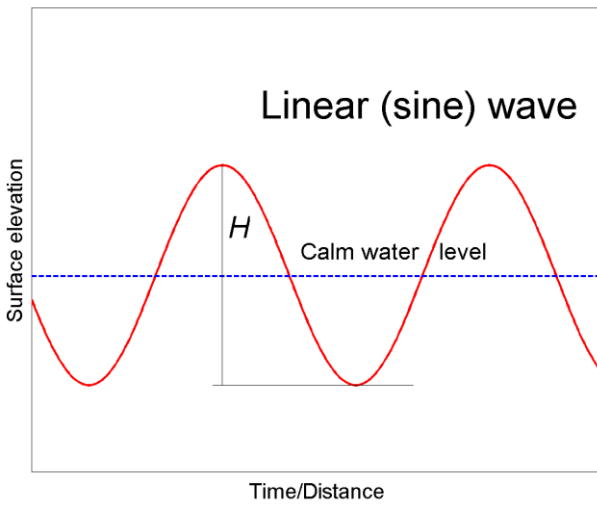
Fig. 2. Extract of Draupner time series close to the extreme wave.

Linear waves – cnoidal waves – solitons

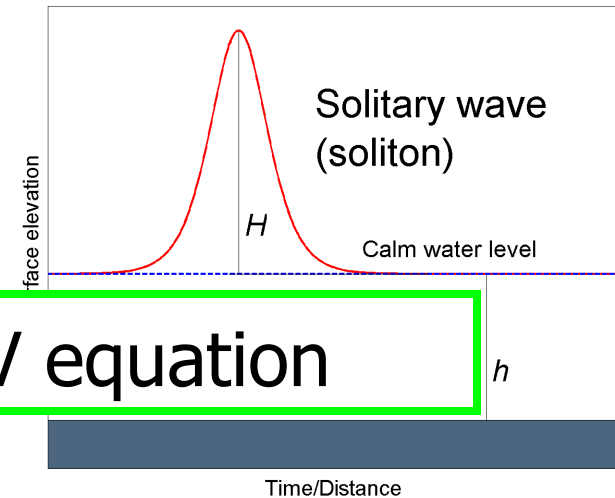
smaller waves,
almost linear

higher waves, more nonlinear

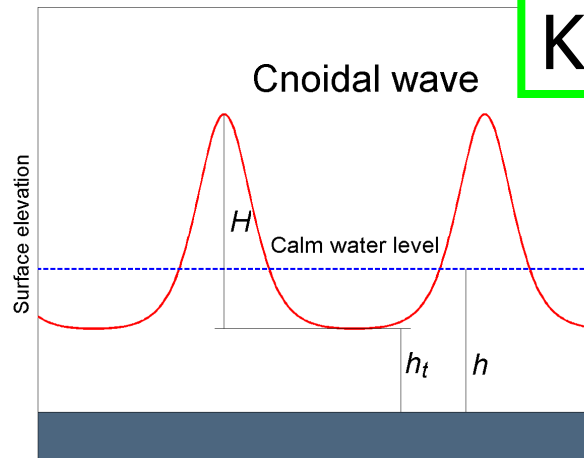
$$\eta = \frac{1}{2} k^2 \cosh^{-2} \left(\frac{1}{2} kx \right)$$



Long waves in shallow water can be described with the use of the **cnoidal** wave theory



KdV equation



Traditionally, Airy (co)sine wave theory is used for water waves

Very long waves in shallow water can be associated with solitary waves

Name: from Jacobi elliptical functions sn, cn, dn



Makers of solitons: contemporary fast ferries

Vessel waves – threat or treasure?

- different from wind waves
- model of monster waves and tsunamis
- model of destructive (wave) climate changes

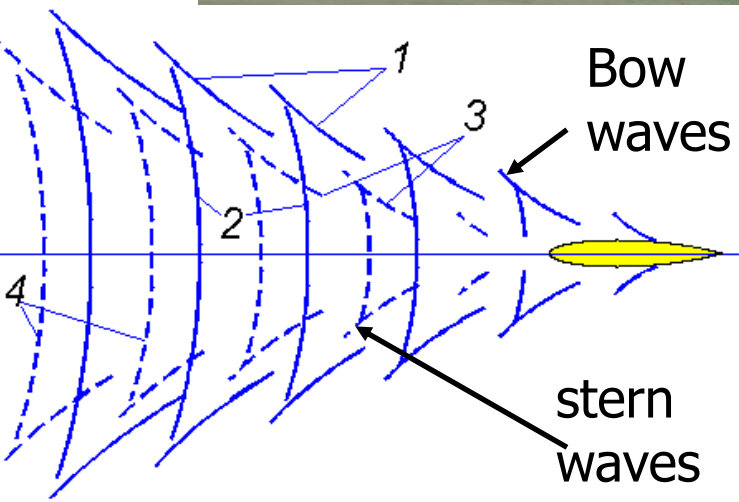


Classical ship wave pattern

Wave heights moderate

Wave crests relatively short

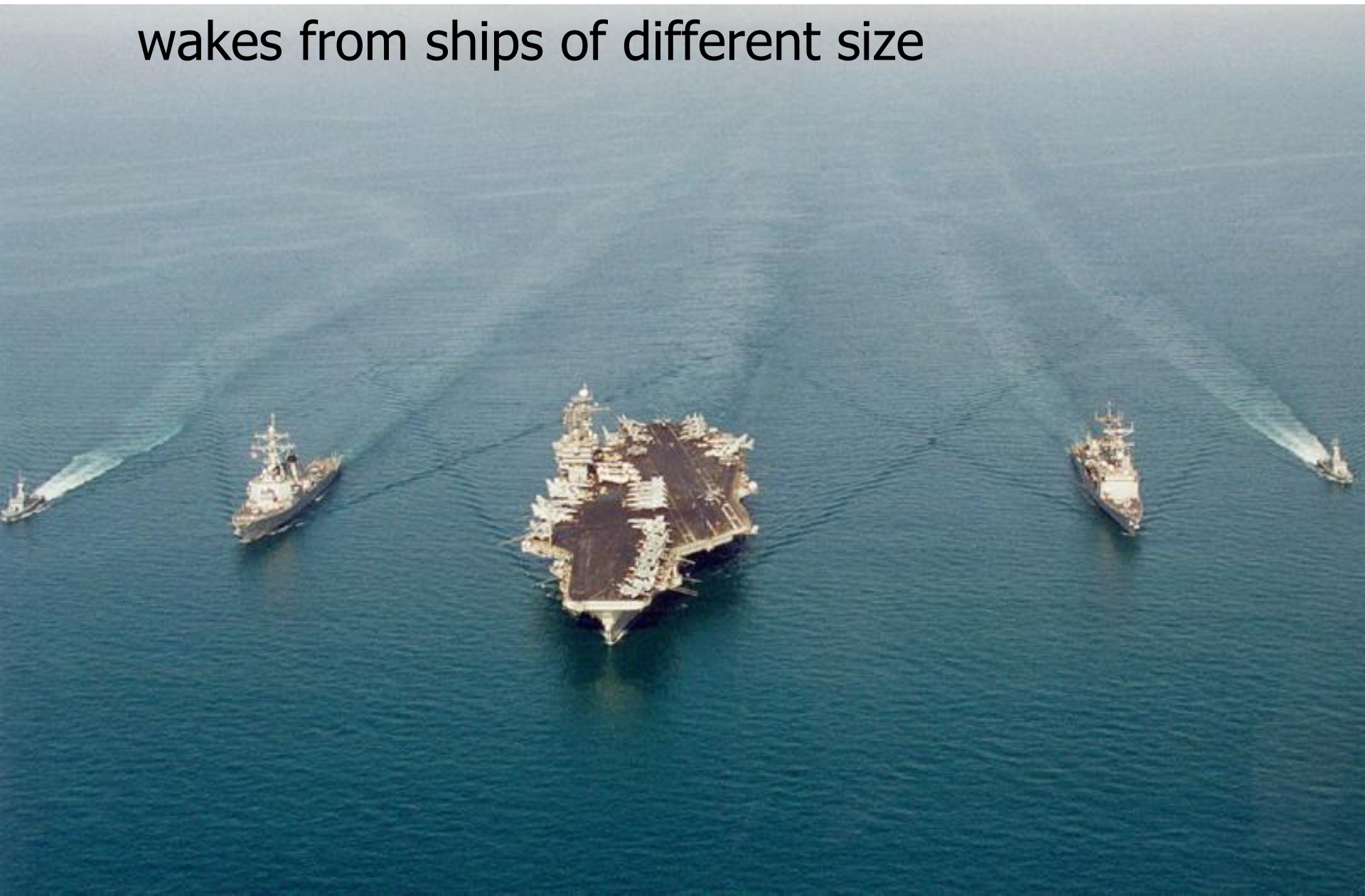
Kelvin theory
of ship waves



(Geirangerfjord, Norway)



There is no difference between
wakes from ships of different size



... small boats .



No
disturbance
ahead

... or duck
or swan
waves

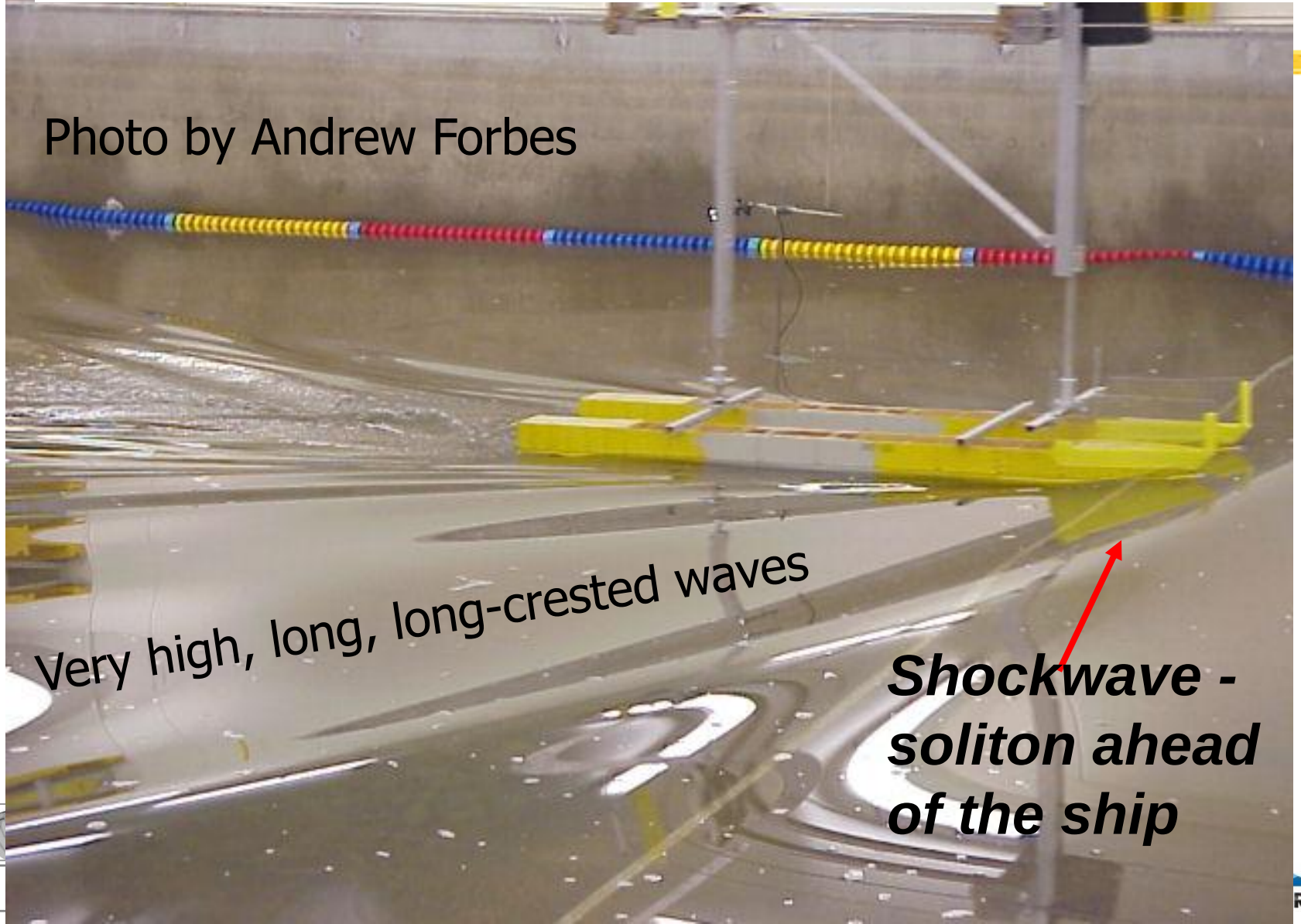


Each single
crest is short



... unless the disturbance moves at a large speed in shallow water

Photo by Andrew Forbes



Very high, long, long-crested waves

***Shockwave -
soliton ahead
of the ship***



The source of difference

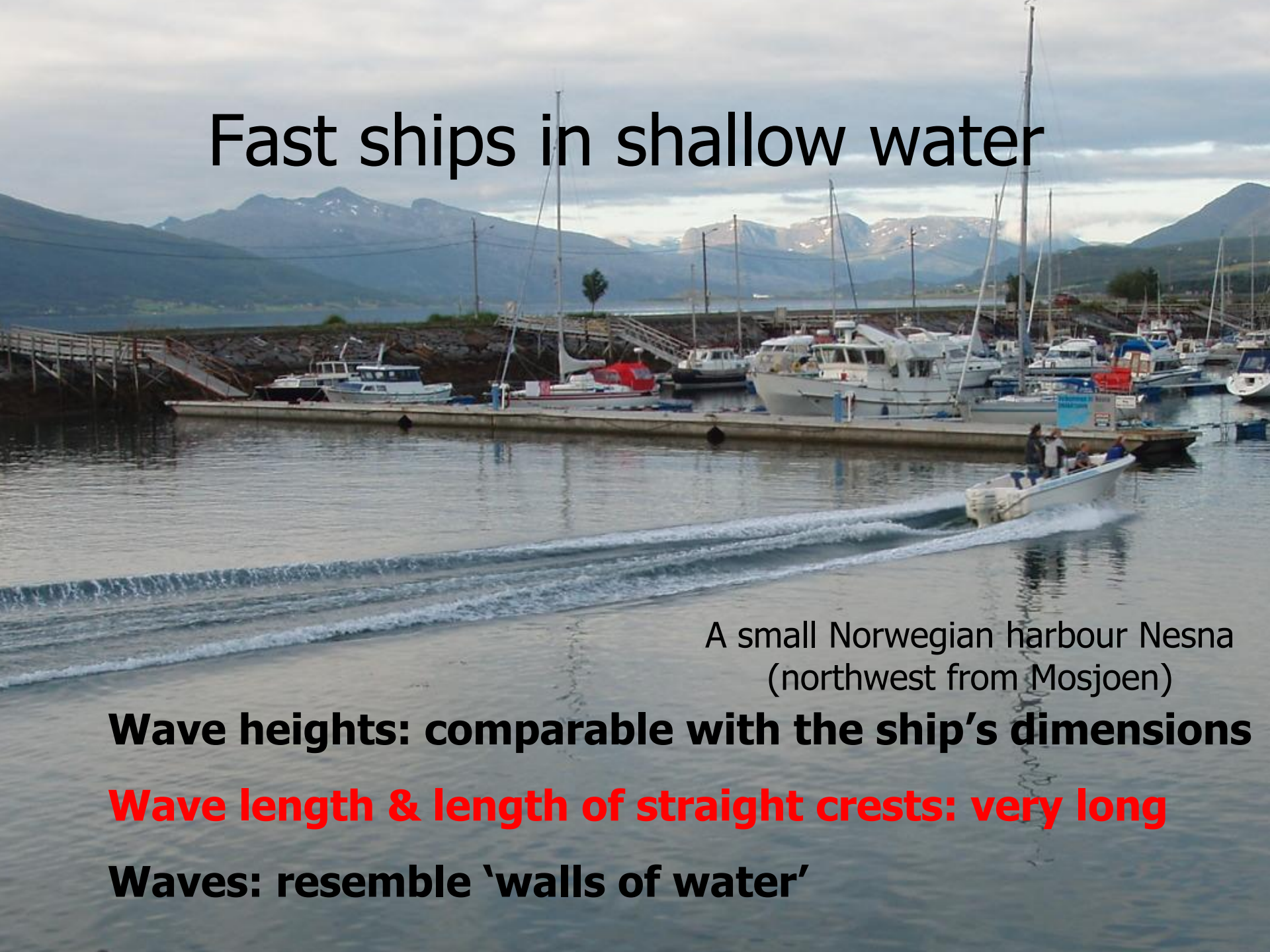
The decisive factor:

- not speed alone
- but **speed *versus* water depth**

FAST FERRIES

- Generation of long & long-crested waves
- In shallow water: phase speed == group speed
- both only depend on the depth

Fast ships in shallow water



A small Norwegian harbour Nesna
(northwest from Mosjoen)

Wave heights: comparable with the ship's dimensions

Wave length & length of straight crests: very long

Waves: resemble 'walls of water'



Ship wave in Broadwater (Gold Coast, ICS 2007 field trip) approaching a seawall



... and overtopped it



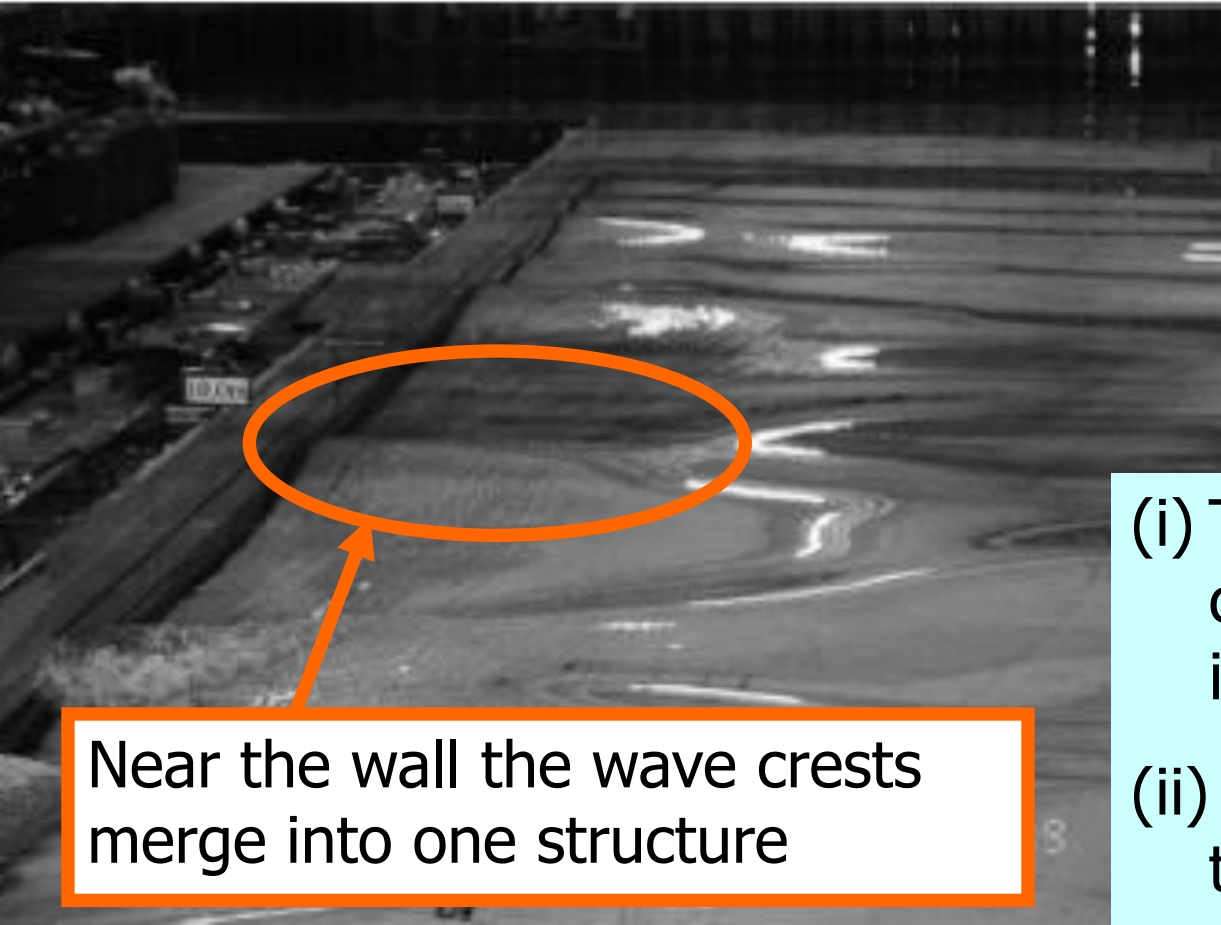
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If a large-amplitude wave reflects from a wall: Mach stem



Near the wall the wave crests merge into one structure

- (i) The length of the common crest gradually increases
- (ii) and frequently is higher than 2x incoming wave

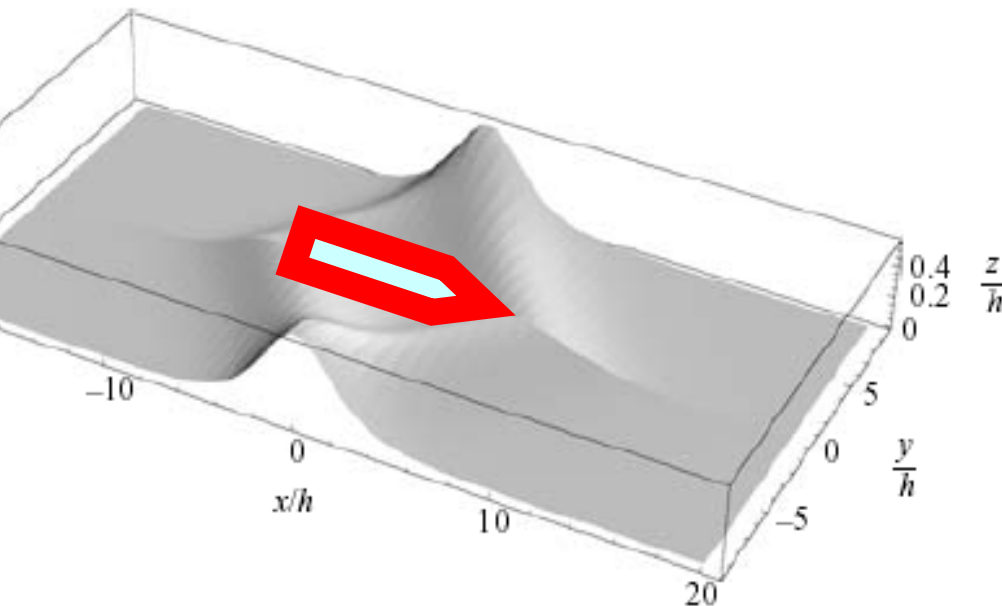
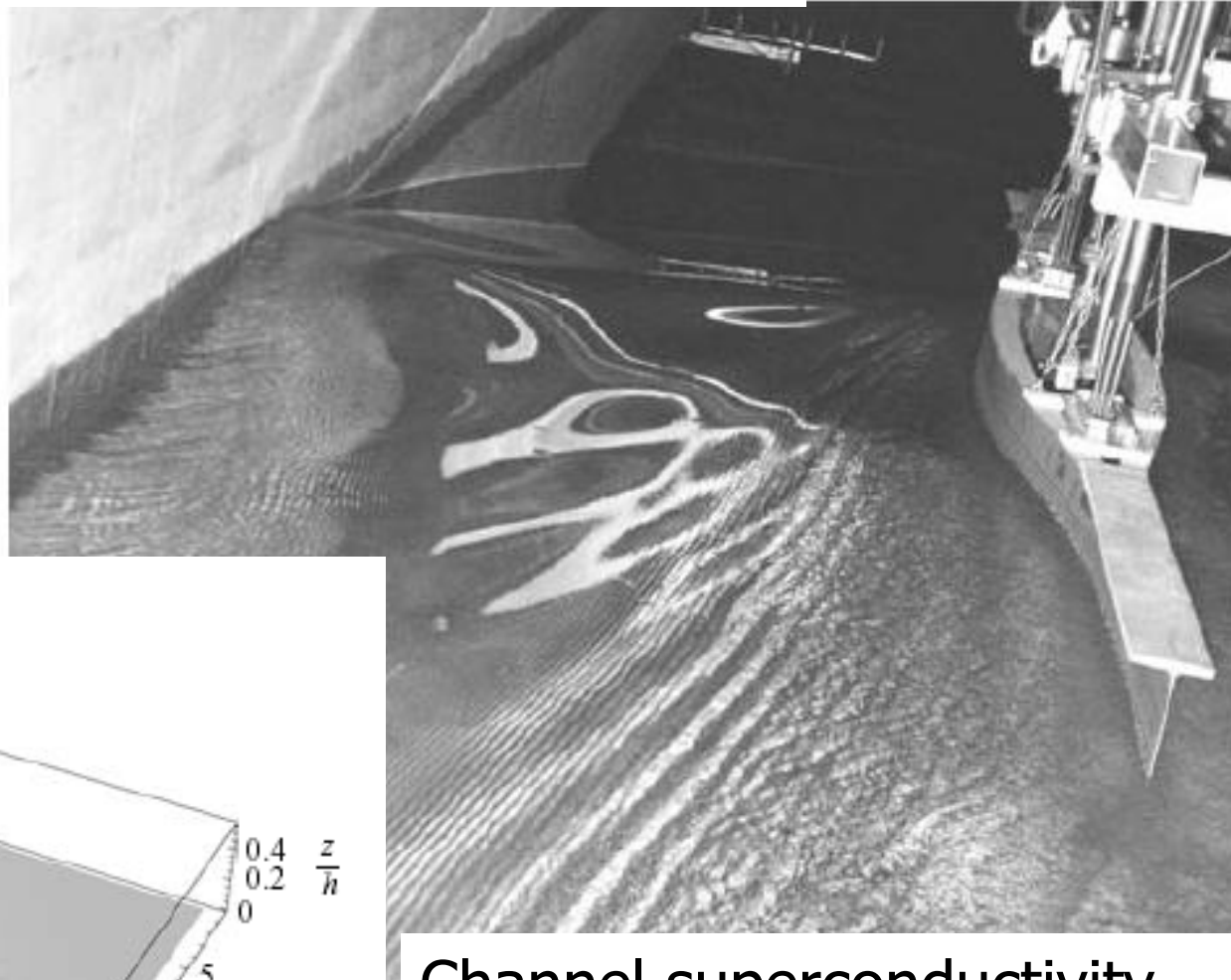
(Yue and Mei 1980,
Pedersen, 1990s)

Mase, Memita, Yuhi, Kitano, Stem waves along vertical wall due to random wave incidence, Coastal Engineering 44 (2002) 339–350



Stable & symmetric case: when a KdV soliton reflects from a wall:

The effect can be used for zero wave resistance in channels: stern wave kills bow waves



Channel superconductivity

Chen, Sharma, Stuntz, *J. Fluid Mech.*, 2003



Pattern of **crossing ship waves**:

- (i) Wave crests bend
- (ii) Wave heights increase



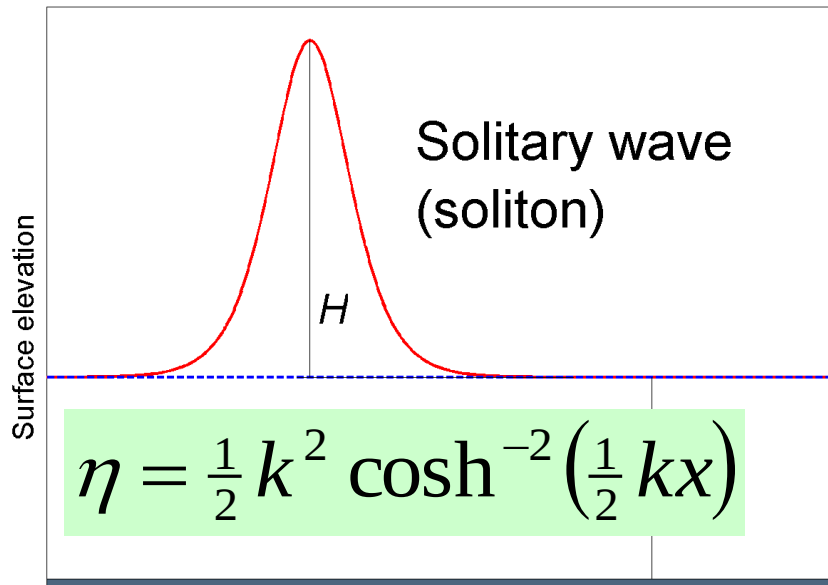
**KdV**

Crossing solitons

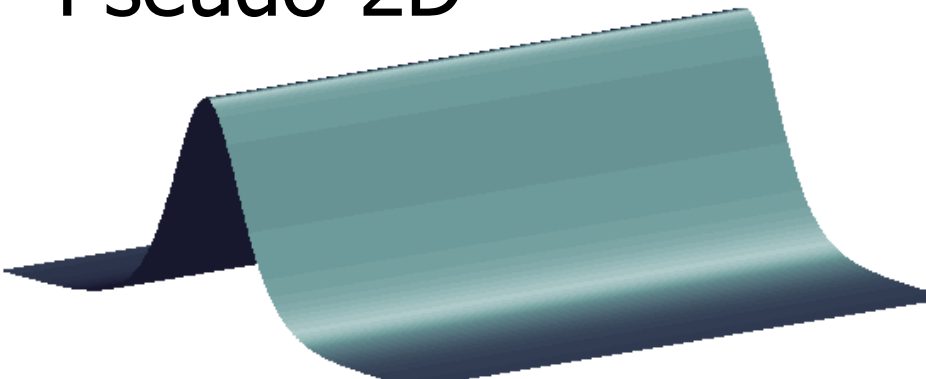
KP

Korteweg & de Vries (1895)

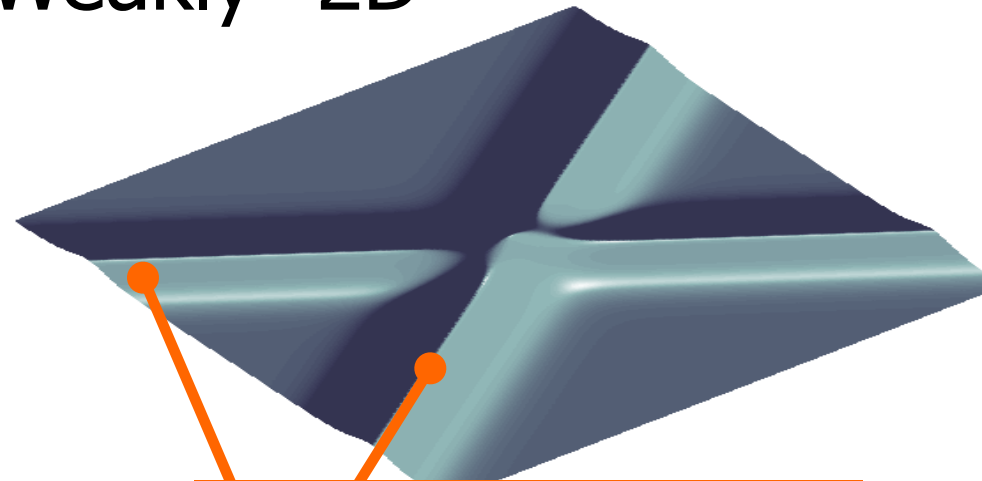
Kadomtsev & Petviashvili (1970)



Pseudo-2D



"Weakly" 2D

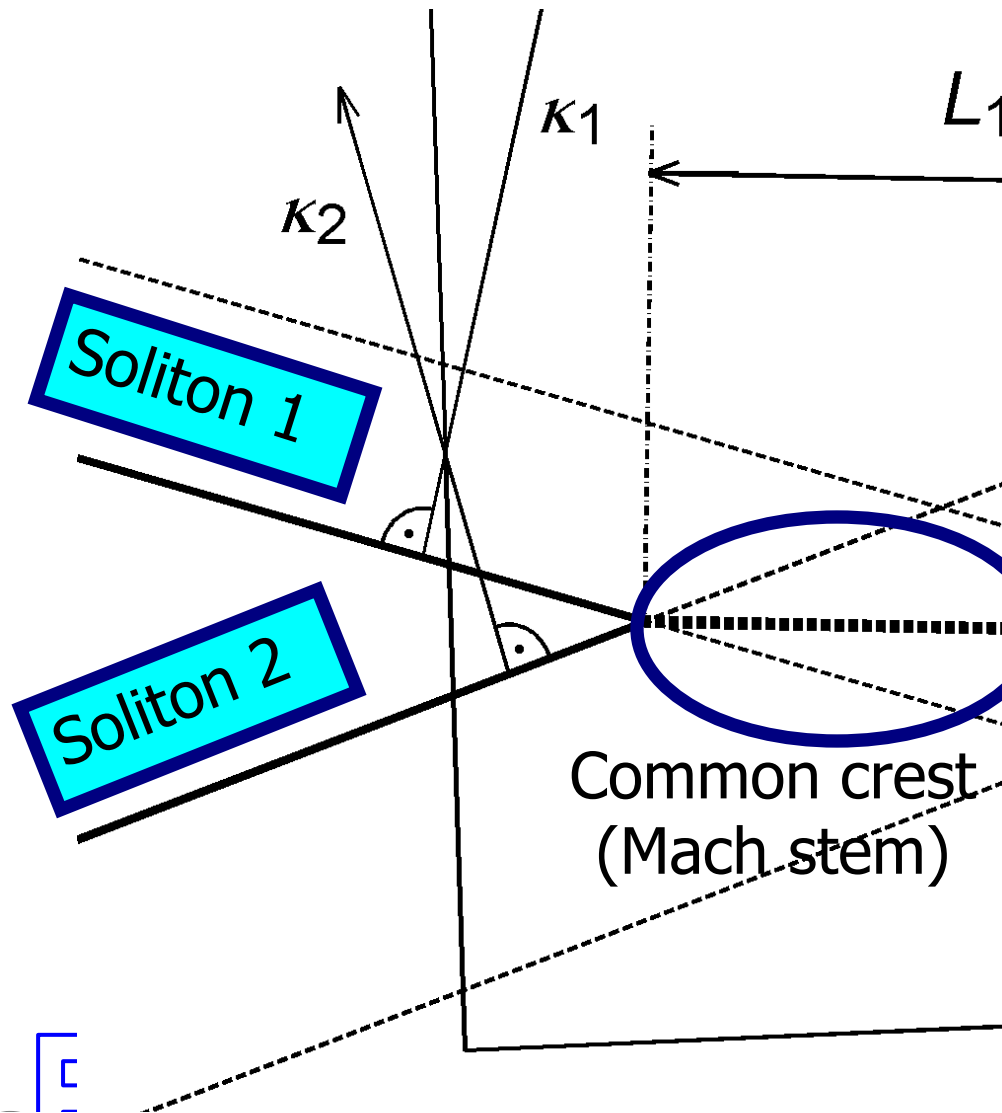


Single waves are KdV solitons

Overview of soliton interactions:
Soomere, in: Encyclopedia of
Complexity and Systems Science,
Springer 2009, vol. 9, 8479–8504

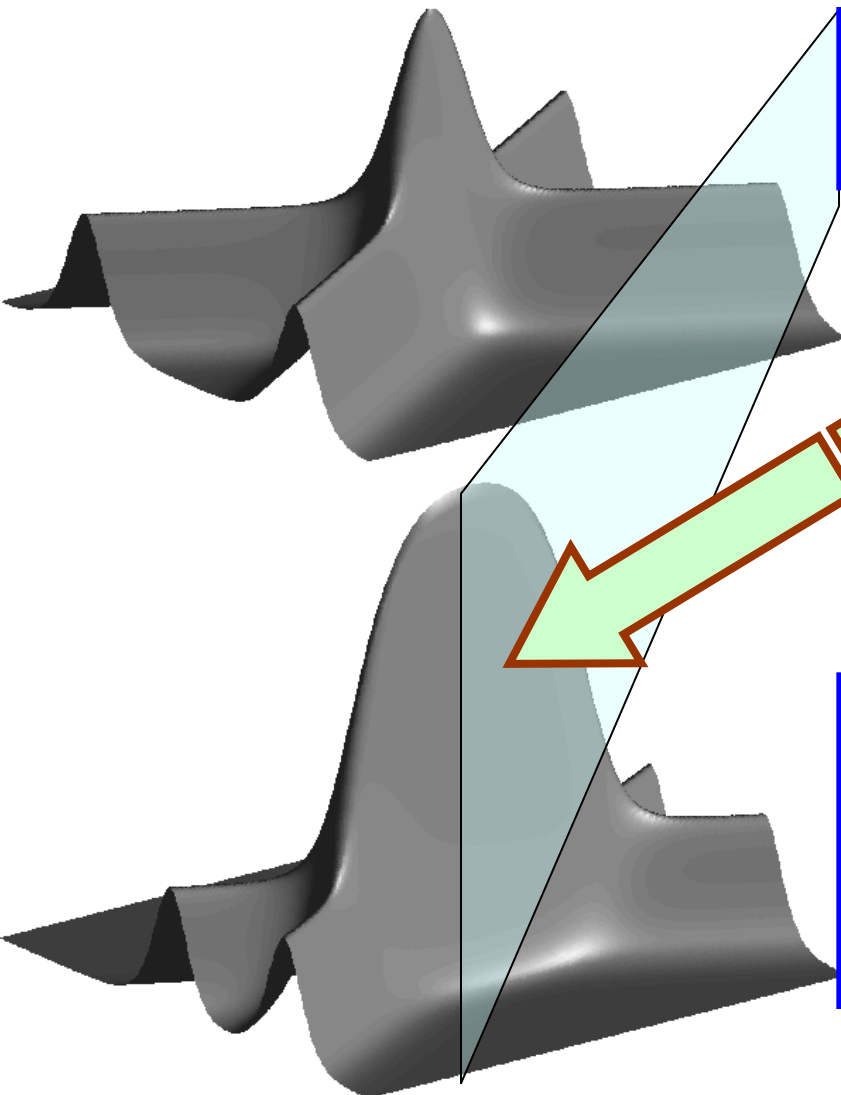


If there is no wall: phase shift & high common crest





Drastic variations of the elevation pattern for different crossing angles



(i) Up to 4-fold increase in the maximum elevation

Miles, *J. Fluid Mech.* 1977

(ii) The **slope** may **8x** exceed the slope of single solitons

Soomere & Engelbrecht, *Wave Motion* 2005; *Eur. J. Mech. B/Fluids* 2006

(iii) The orientation of the crest of both the solitons changes: waves may come from another / unexpected direction

Soomere, *Phys. Lett. A* 2004



Very steep waves tend to break ...



Walter Crane, Horses of Neptune, 1892



Usually, ship in rough seas tries to face waves with its bow – the most reliable part

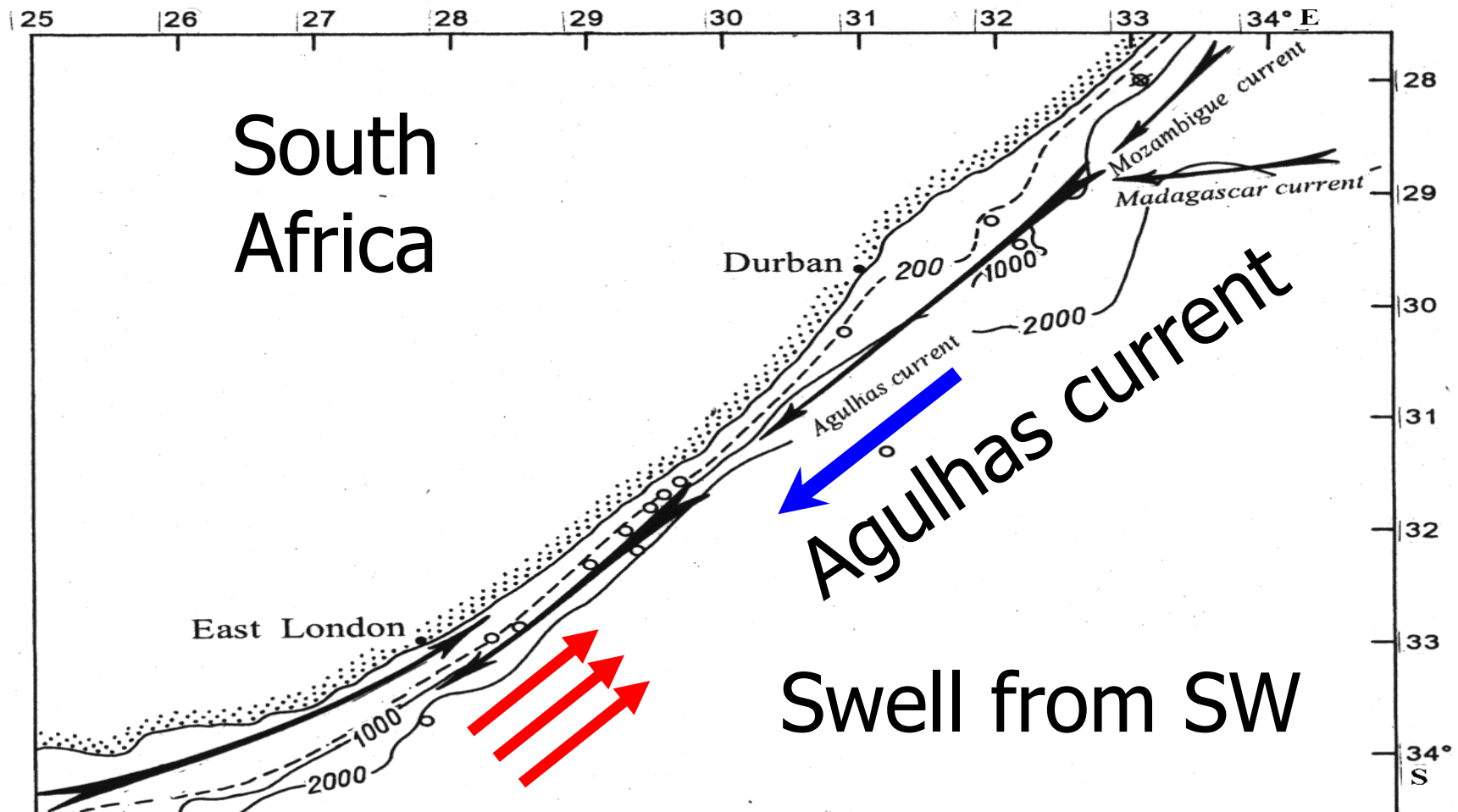
Waves approaching from an unexpected direction: particularly dangerous

Scuttlebutt Photos: Big Waves
provided by Donald Brewster - We can't vouch for the validity of these photos, but they look pretty real, and the waves look pretty big.



Acute & changing danger:

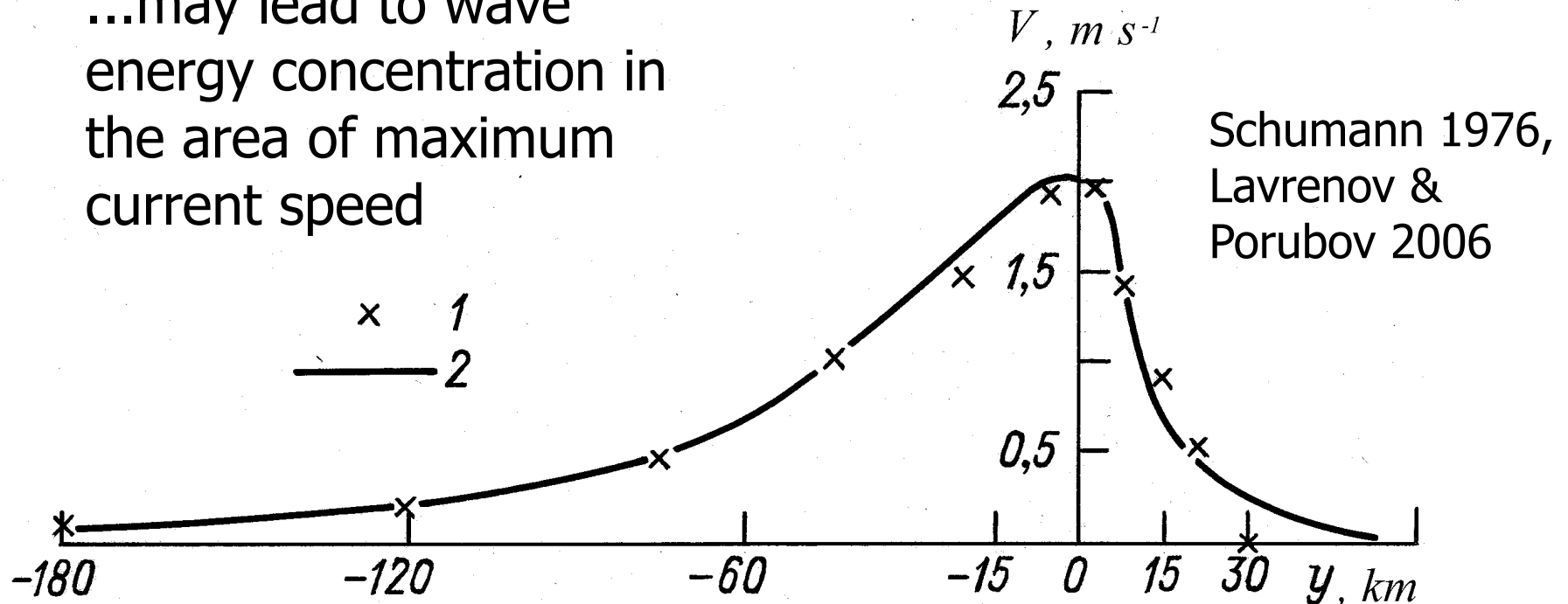
frequently evident in the vicinity of jet currents:
waves running against current become high and steep





Spatial structure of the Agulhas current: waveguide and trap

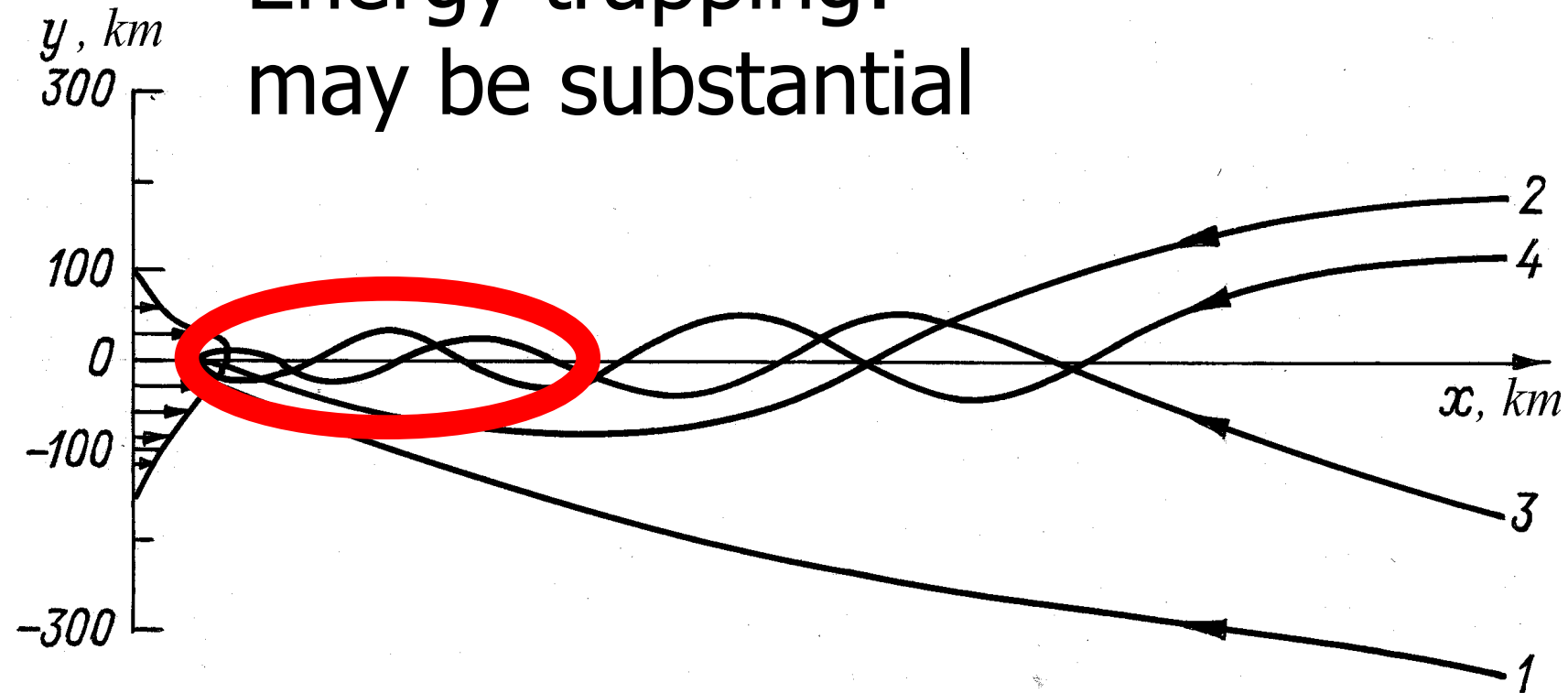
...may lead to wave energy concentration in the area of maximum current speed



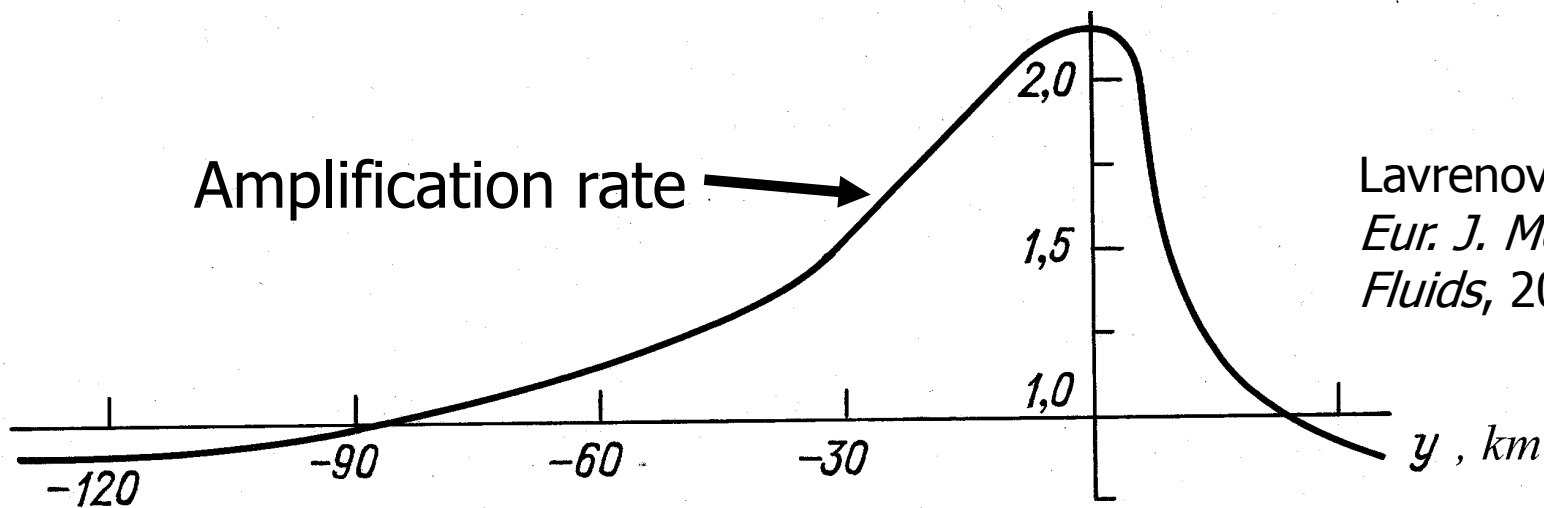
The reason: refraction – tendency of wave rays to turn towards area of larger current velocities – analogue to refraction towards smaller depths



Energy trapping: may be substantial



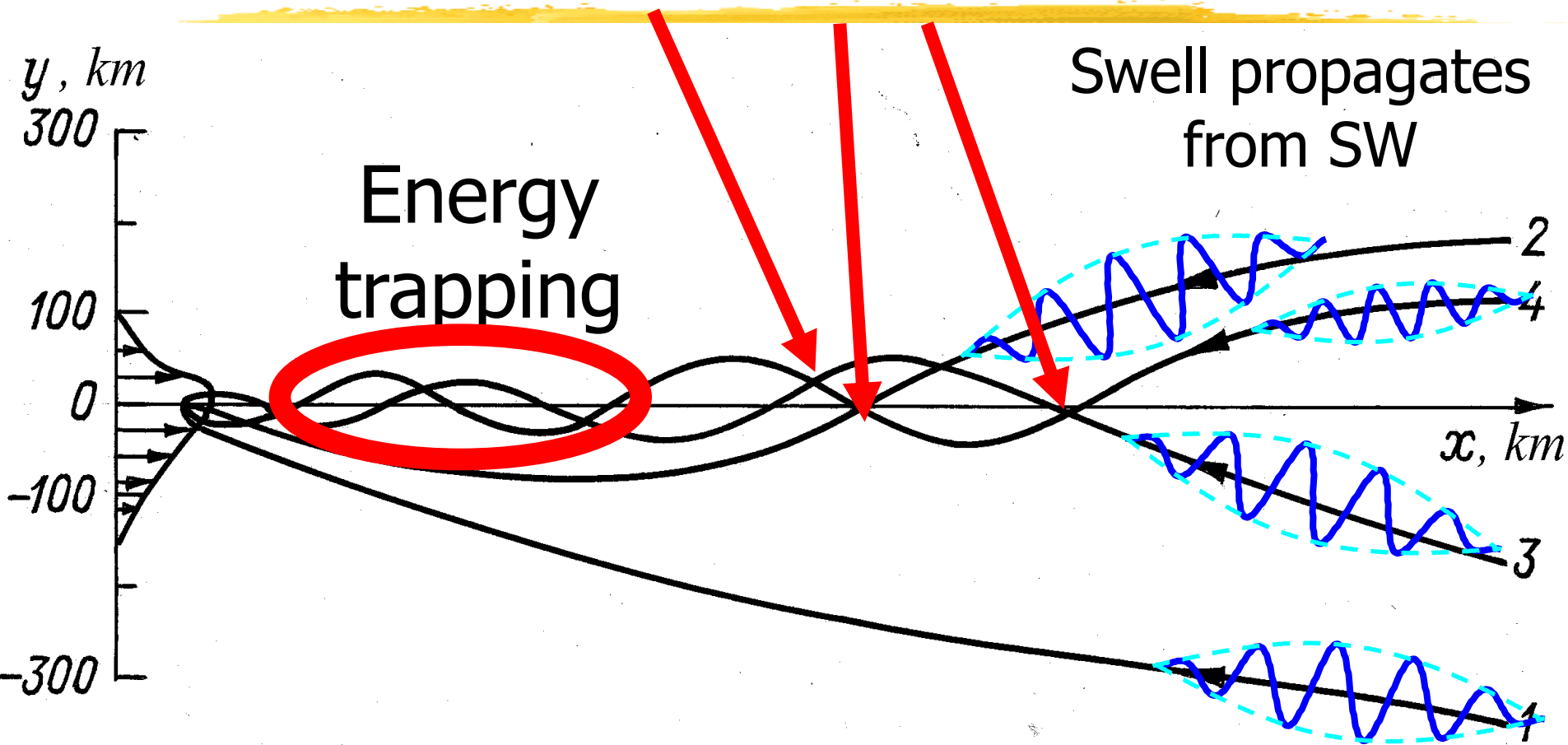
Amplification rate →



Lavrenov, Porubov,
*Eur. J. Mech. B
Fluids*, 2006



Extreme danger: crossing of long waves redirected by refraction



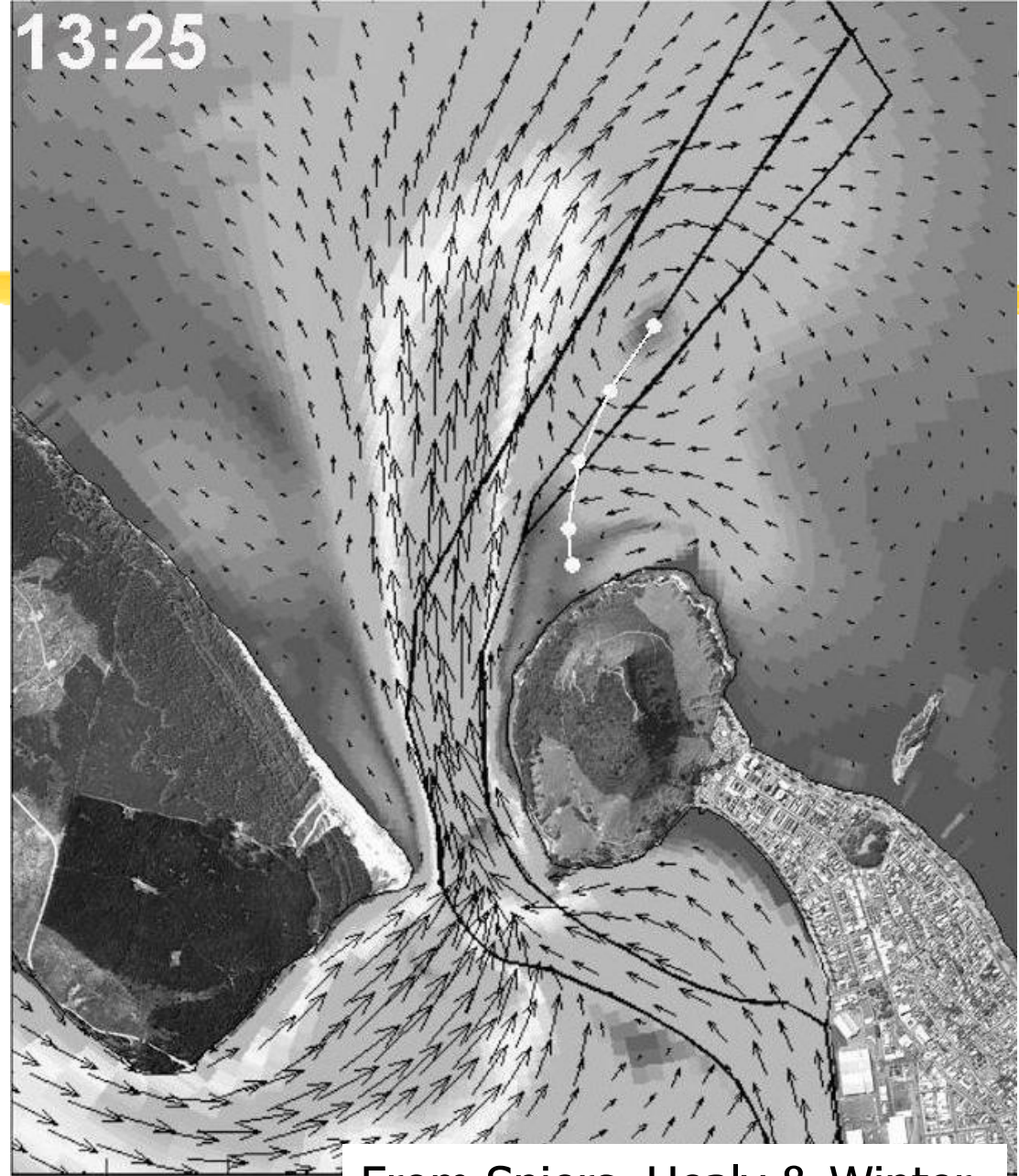
Soomere 2005,
cited in Lavrenov, Porubov, *Eur. J. Mech. B Fluids*, 2006



13:25

No need for
Agulhas:
an ebb jet
would do the
job!

(The closer the ship
is to a harbour,
the more likely it is
hit by a rogue
wave?)



Entrance to
Tauranga Harbour

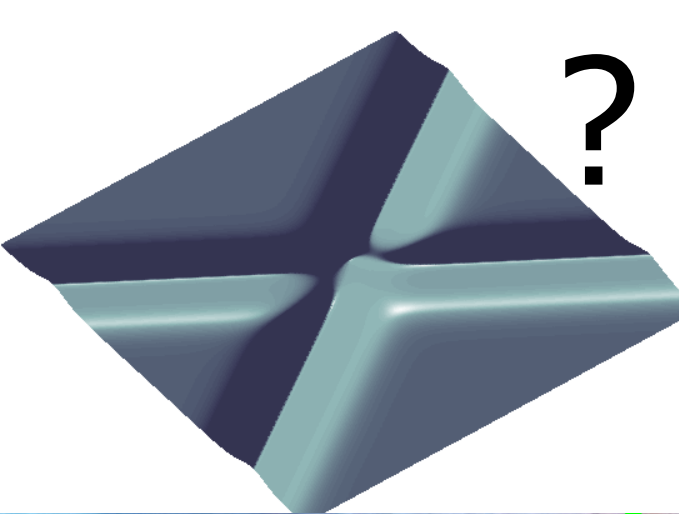
Complexity of Nonlinear

Waves – Tallinn 05.10.2009

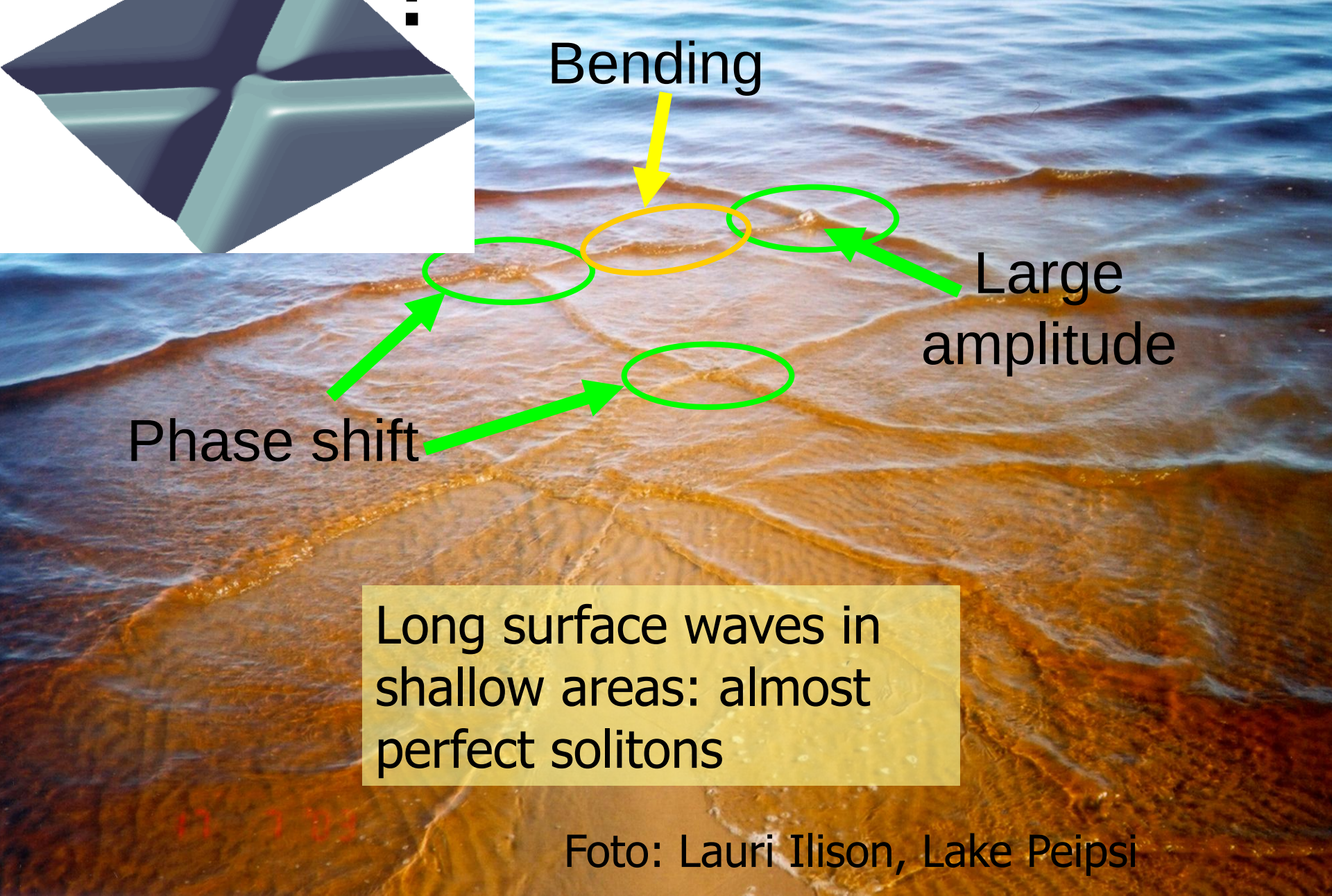
From Spiers, Healy & Winter,
J. Coastal Res. 2008

Institute of Cybernetics

WAVE ENGINEERING



Nature or computer game?



Bending

Large
amplitude

Phase shift

Long surface waves in
shallow areas: almost
perfect solitons

Foto: Lauri Ilison, Lake Peipsi



Living forever? (California)



11.9.2001 08:42



Goat Island, NZ, April 2007



Harilaid Island, Estonia, Sept 2007



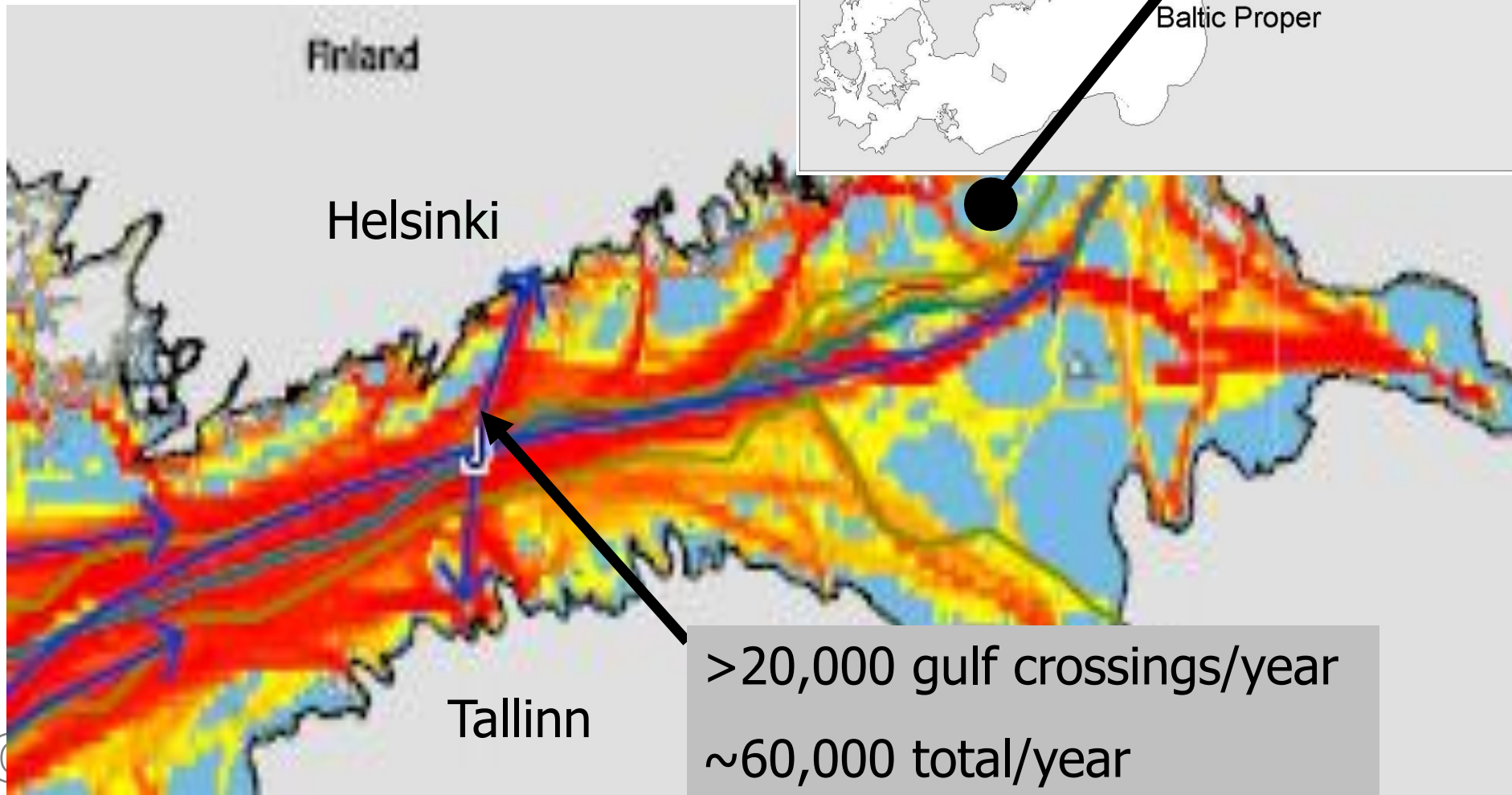


Ship waves: a model of wave climate changes

Possible changes to the wave field

- Heights (incl. extremes and averages)
- Periods / lengths
- Propagation / approach direction
- Internal / group structure
- Presence of monster (giant, rogue) waves

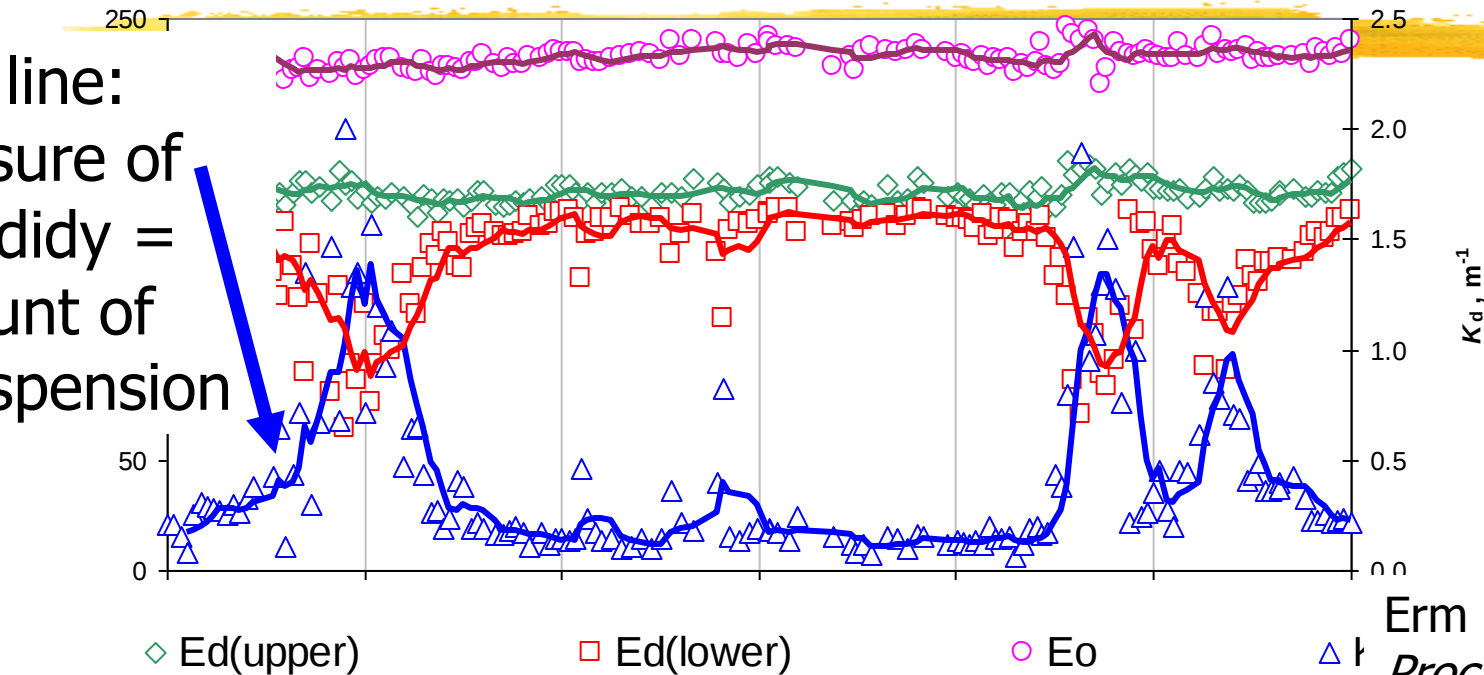
Ship routes in the Gulf of Finland -- a major highway



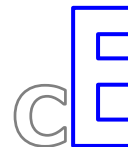
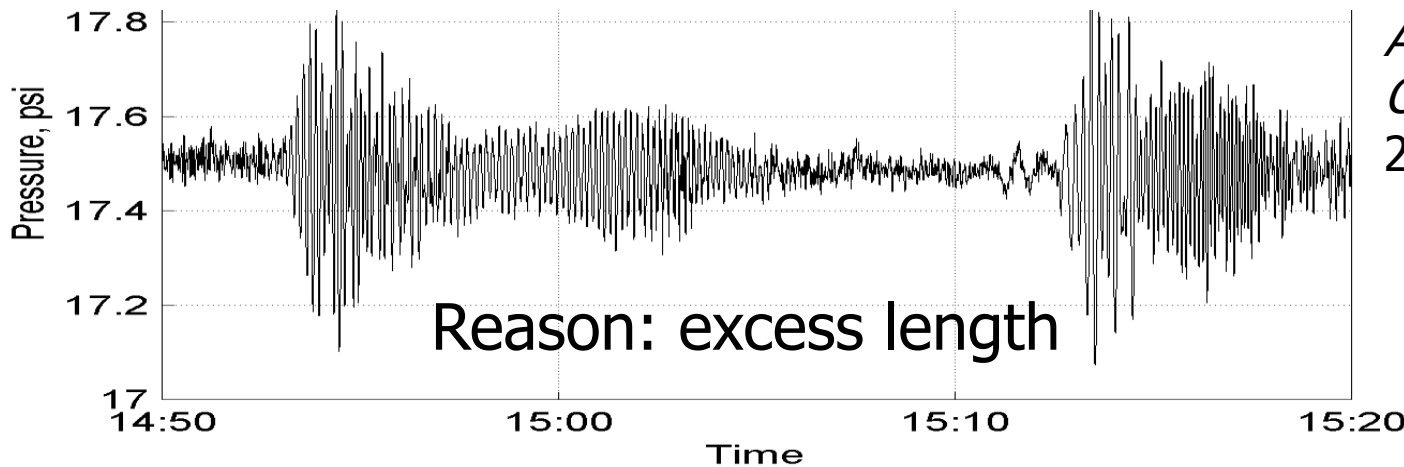


Changes of optical properties of sea water at depth of 5 m: **drastic**

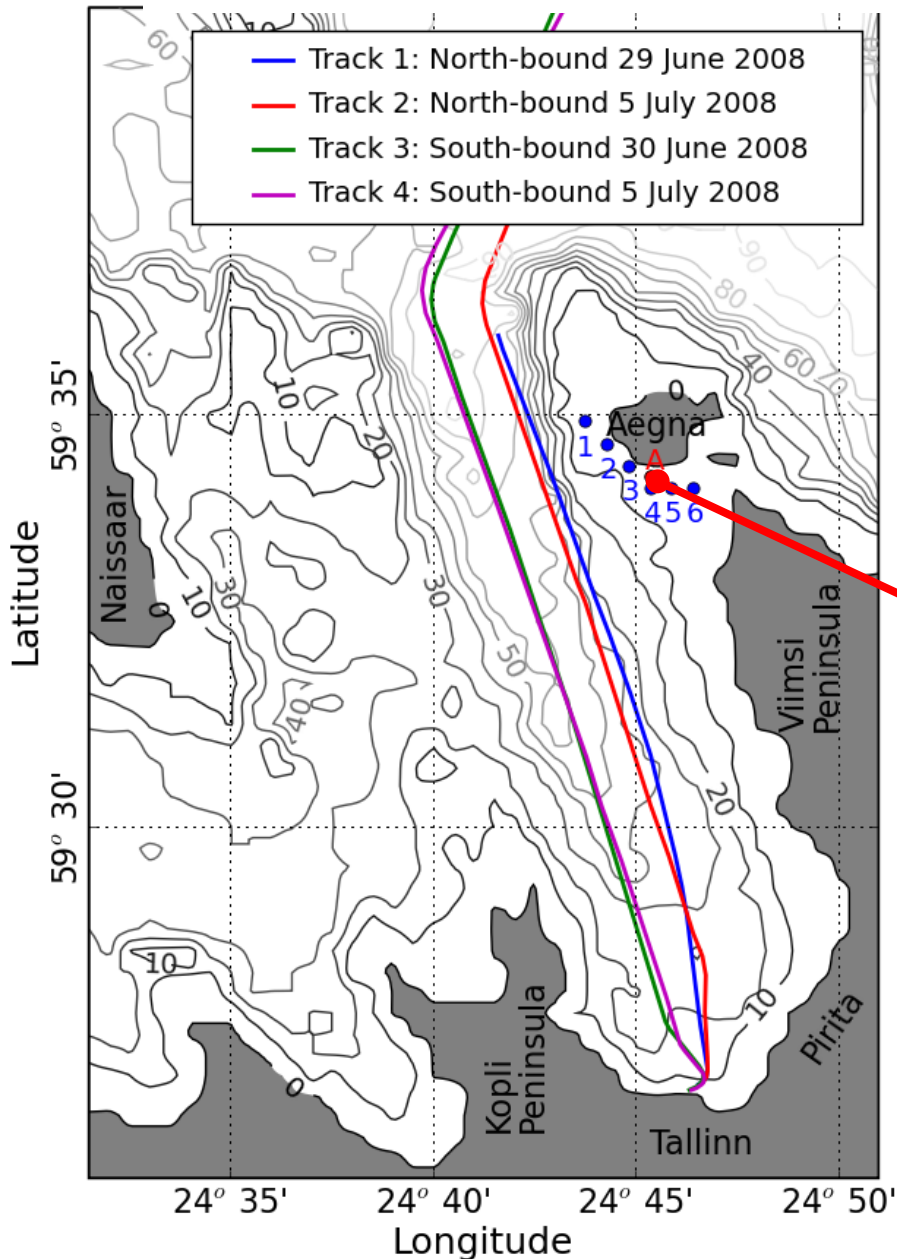
Blue line:
measure of
turbidity =
amount of
resuspension



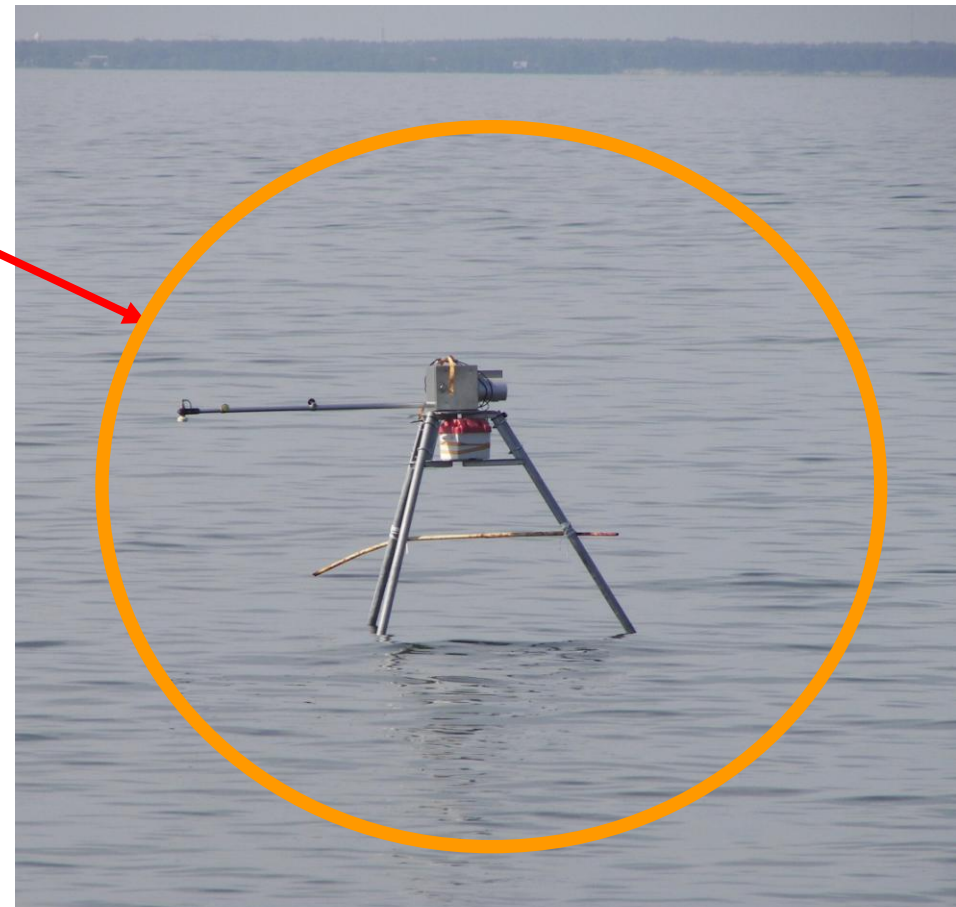
Erm & Soomere,
*Proc. Estonian
Acad. Sci.* 2004;
Oceanologia
2006



Measurements in Tallinn Bay in 2008



Question: How do ship wakes impact the coast?





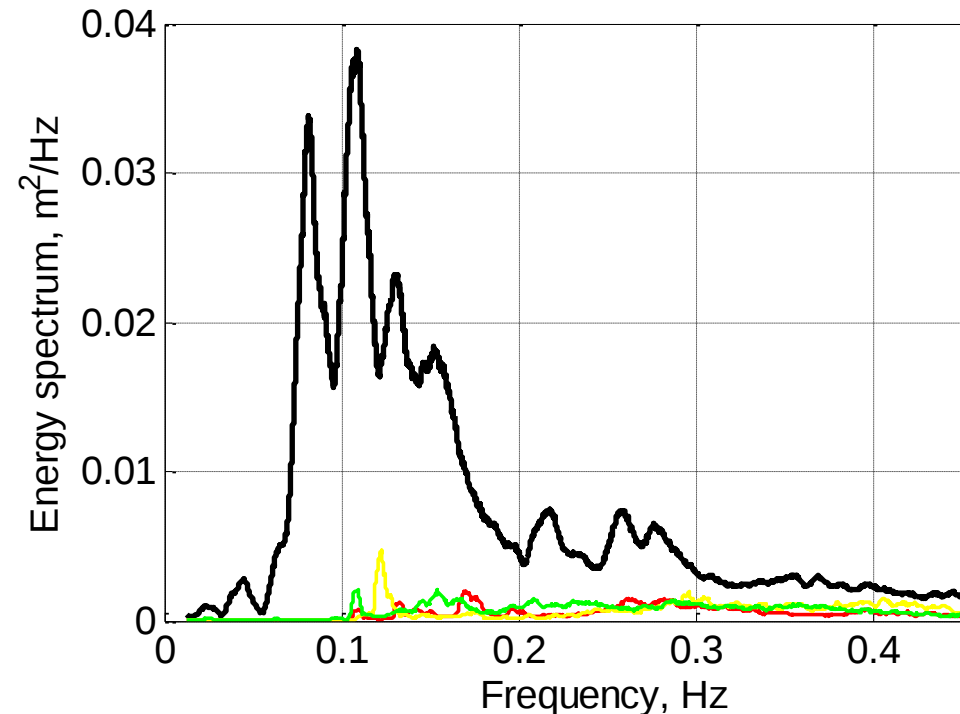
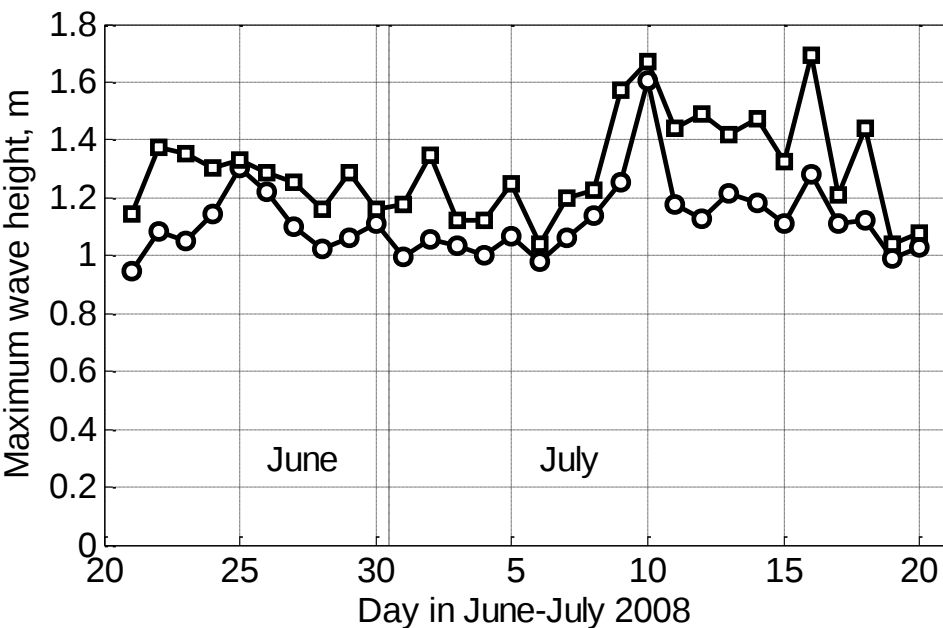
Ship wakes are:

➤ of reasonable height

- Typical highest wave $\sim 0.8\text{--}1\text{ m}$
- $\sim$ top 2-5% of wind waves
- form 5-8% of total wave energy

➤ with very long periods

- Largest ship wave $\sim 10\text{--}15\text{ s}$
- Typical for wind waves 3-4 s

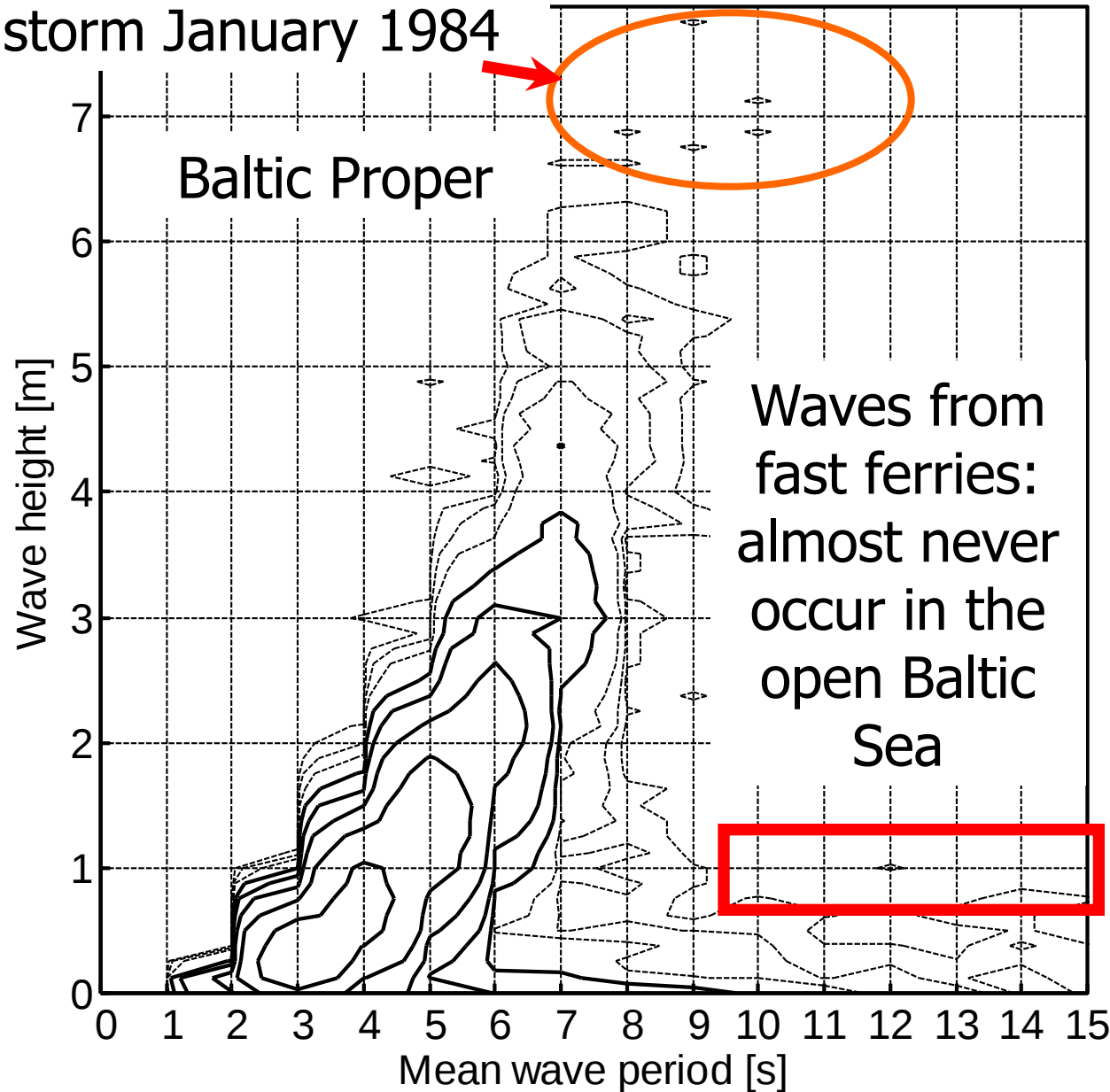




One storm January 1984

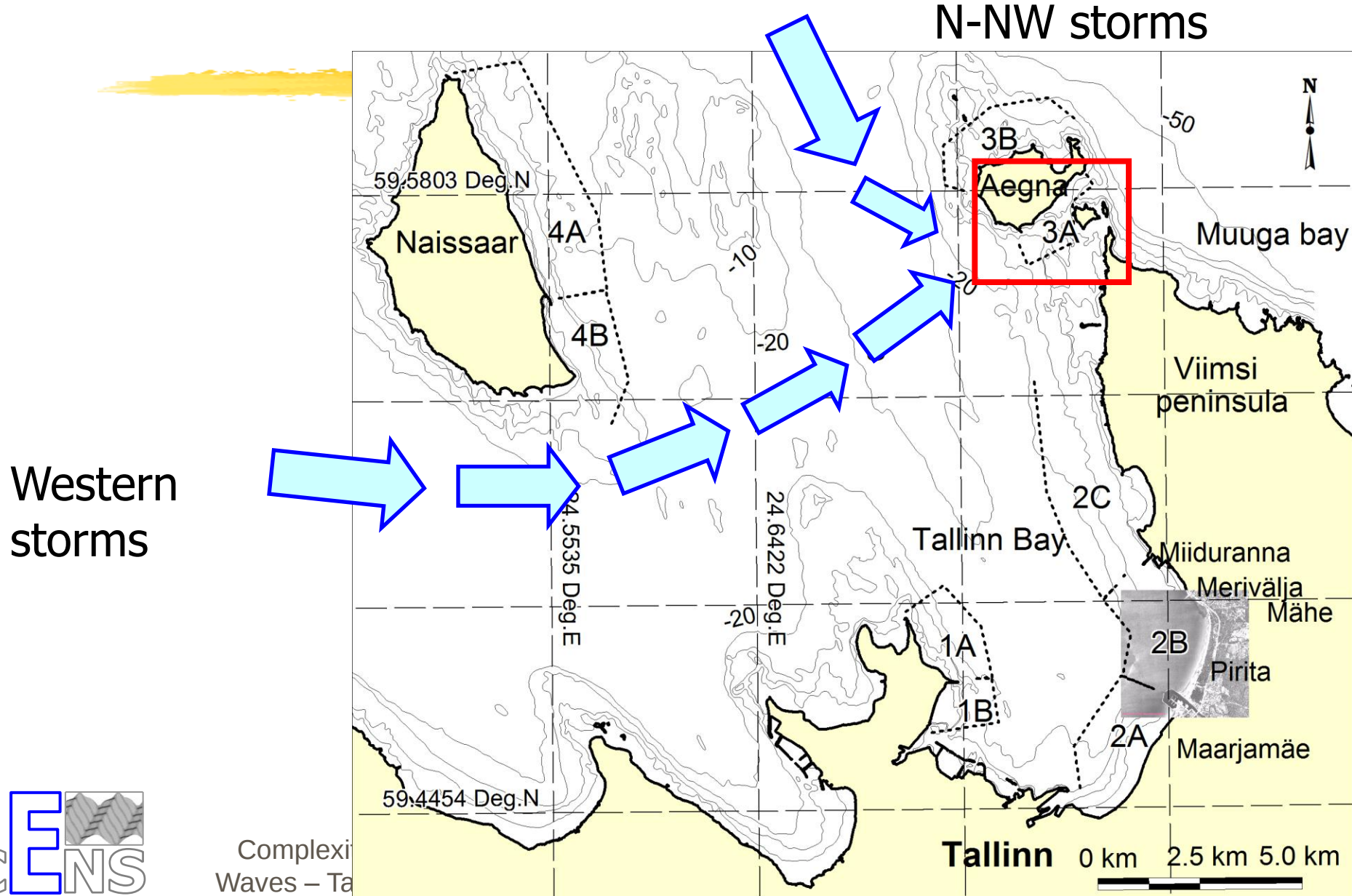
Wave periods in the Baltic Sea: short even for large waves

Isolines for 1, 3,
10, 33, 100, 330,
1000 and 3300
cases,
Almagrundet 1978-
1995 each hour



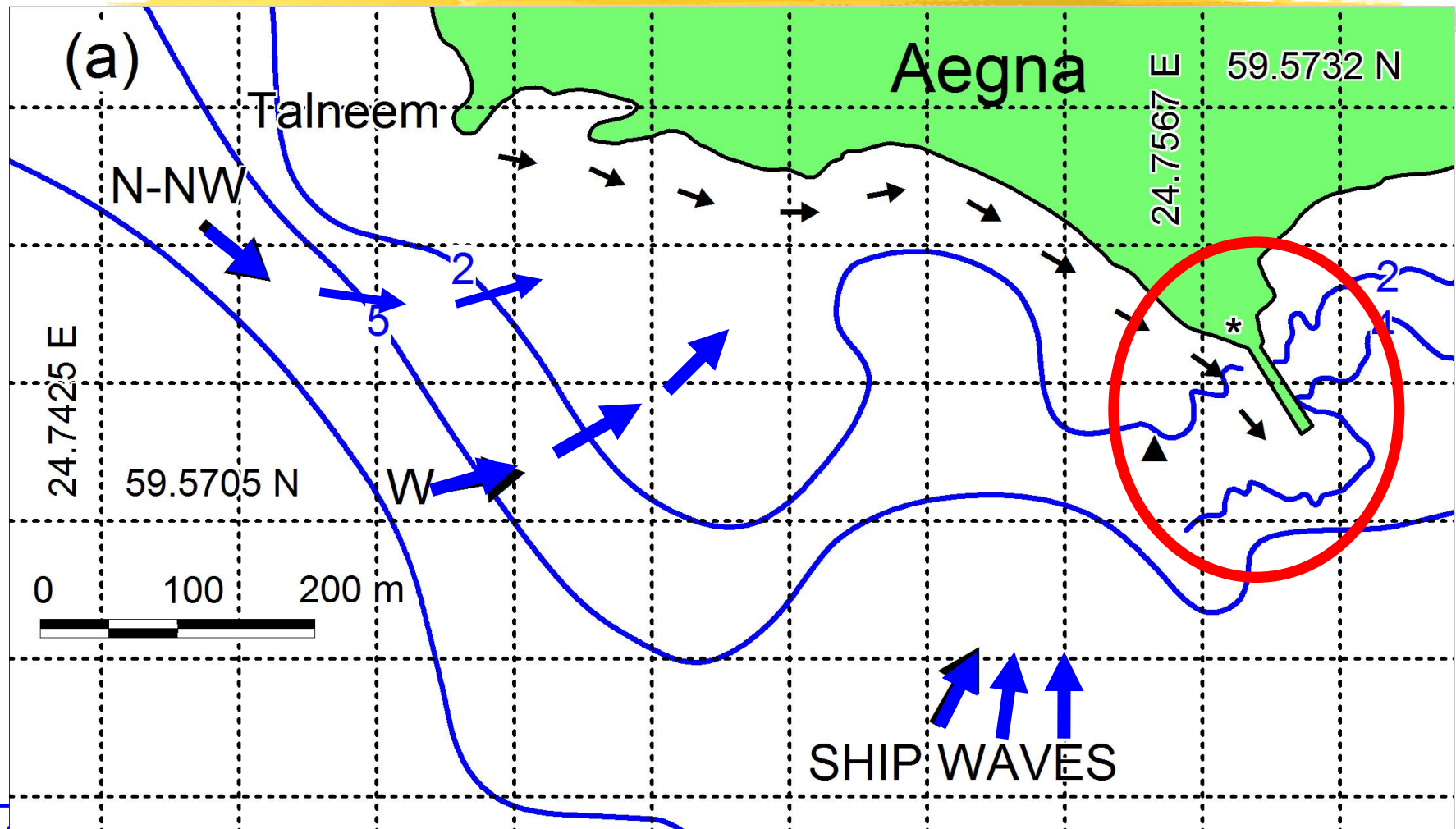


Dominant waves





Natural and vessel-wake-induced transport patterns



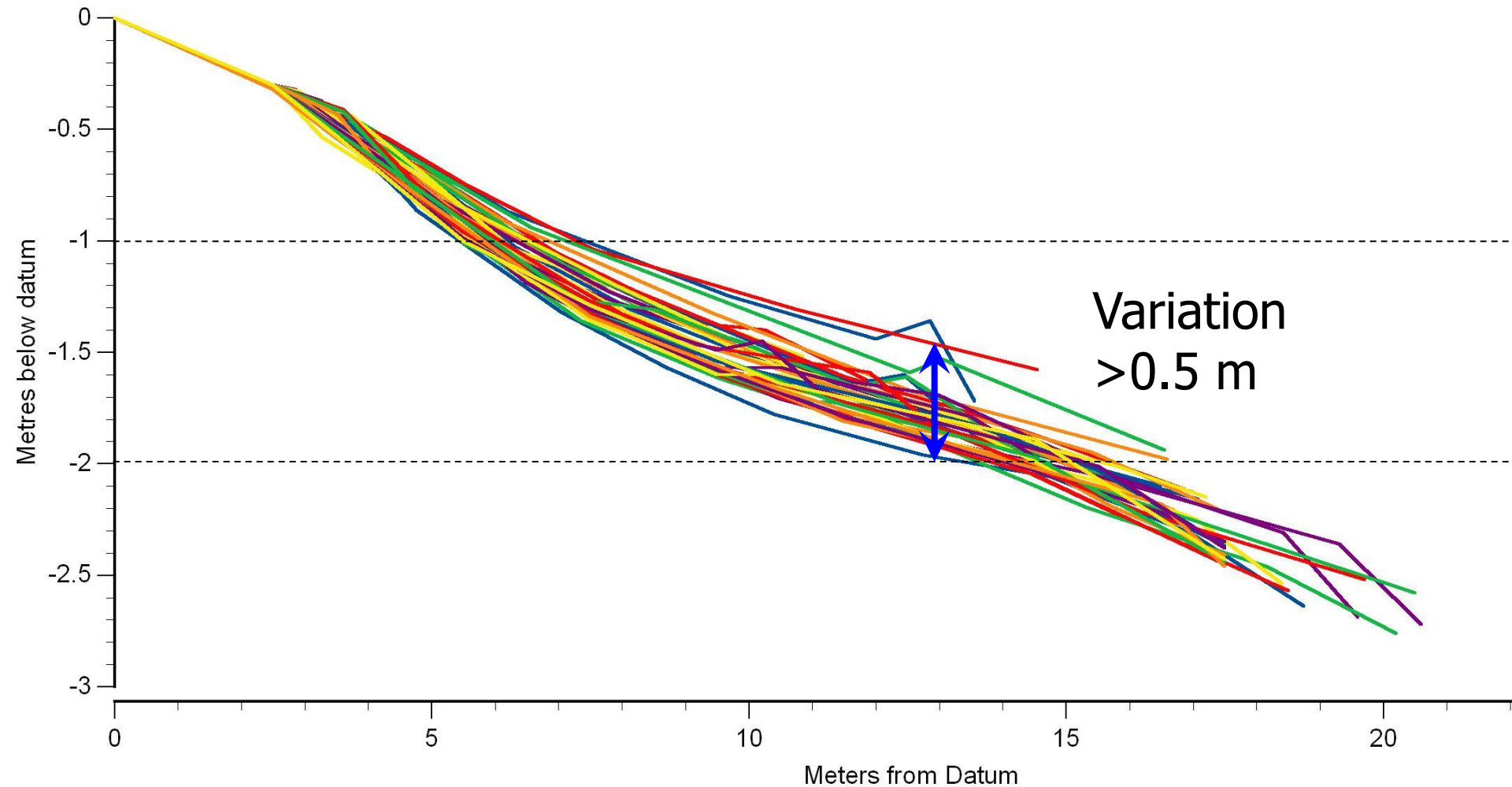
Zero point: a stable boulder

Rapidly changing area

Area not affected by waves during the entire experiment



Variations of the height of the dry beach



Two appearances of the beach



Before

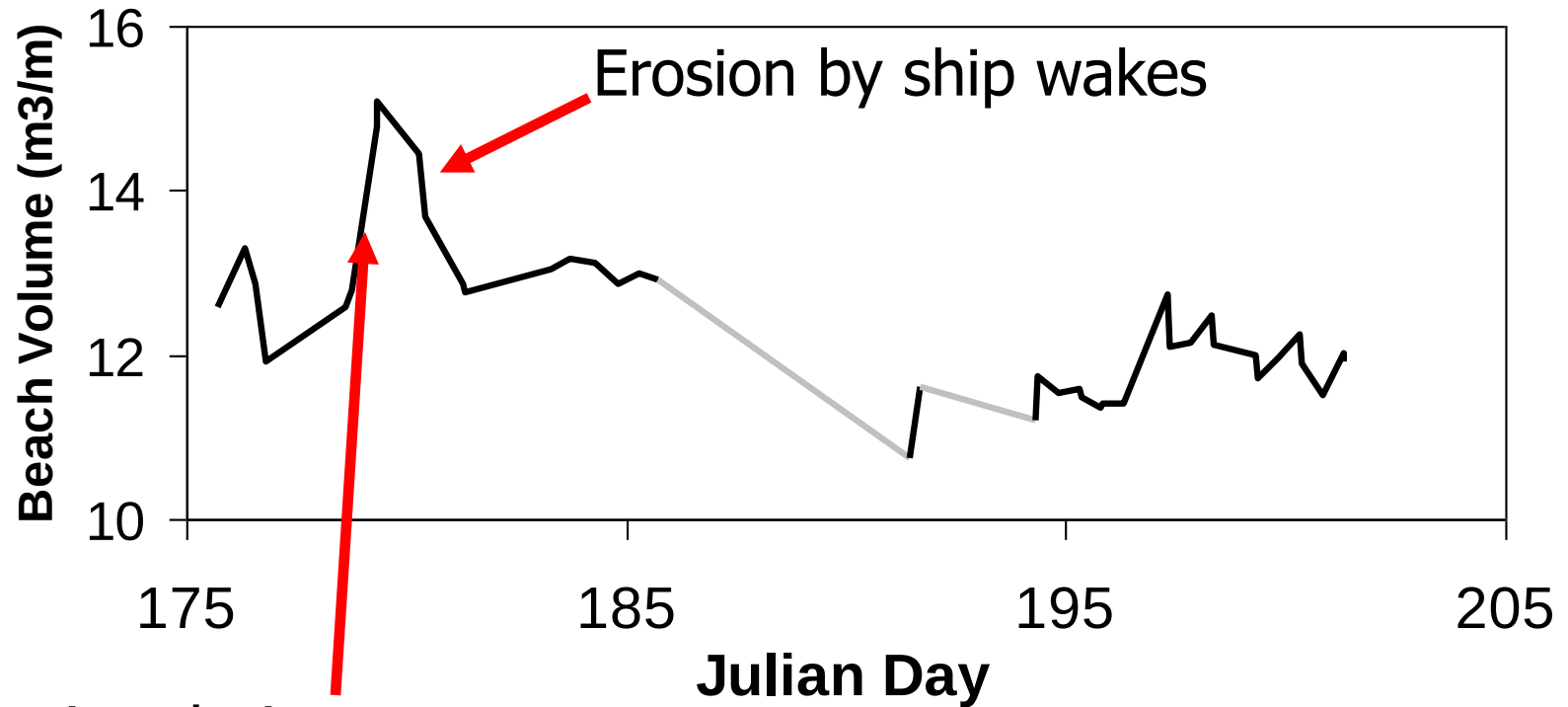


Calm period



After

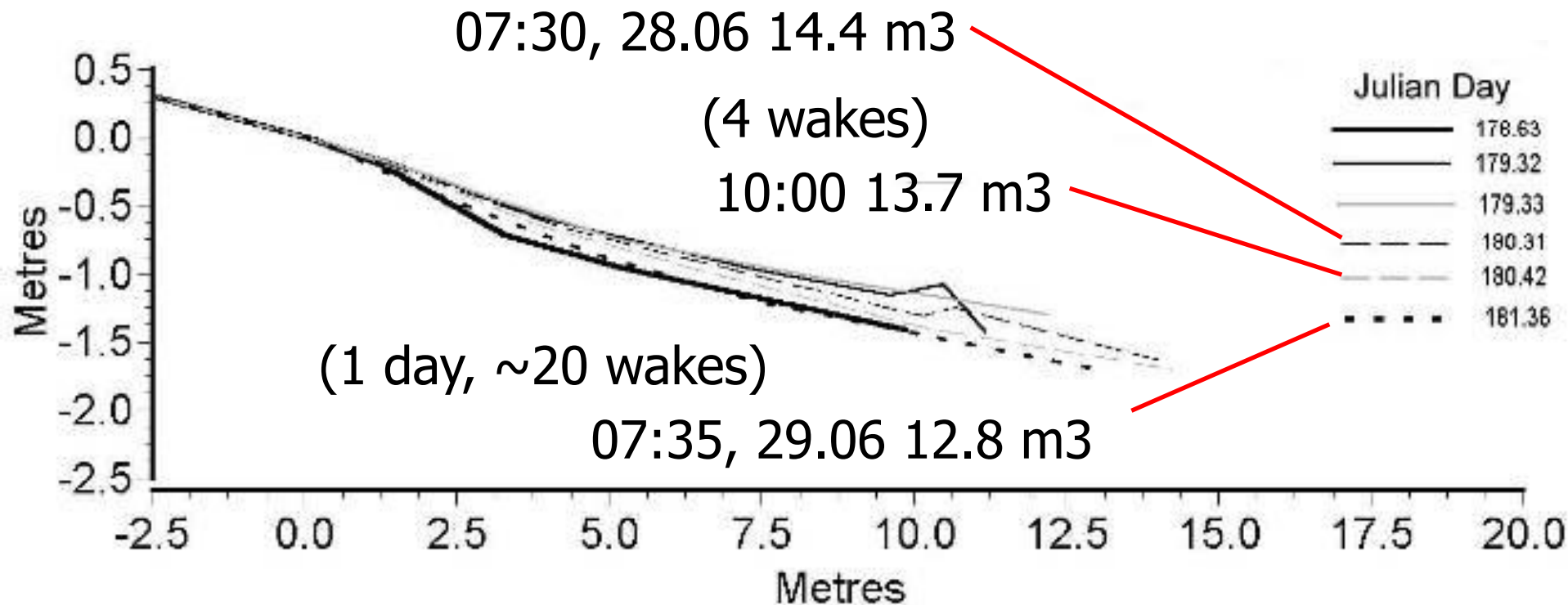
Changes to the dry beach volume



Accretion during a
wave event



Rapid beach response on calm days





Although some ship wakes may move sediment to the West ...





There is no evidence of accretion to the West of the study site

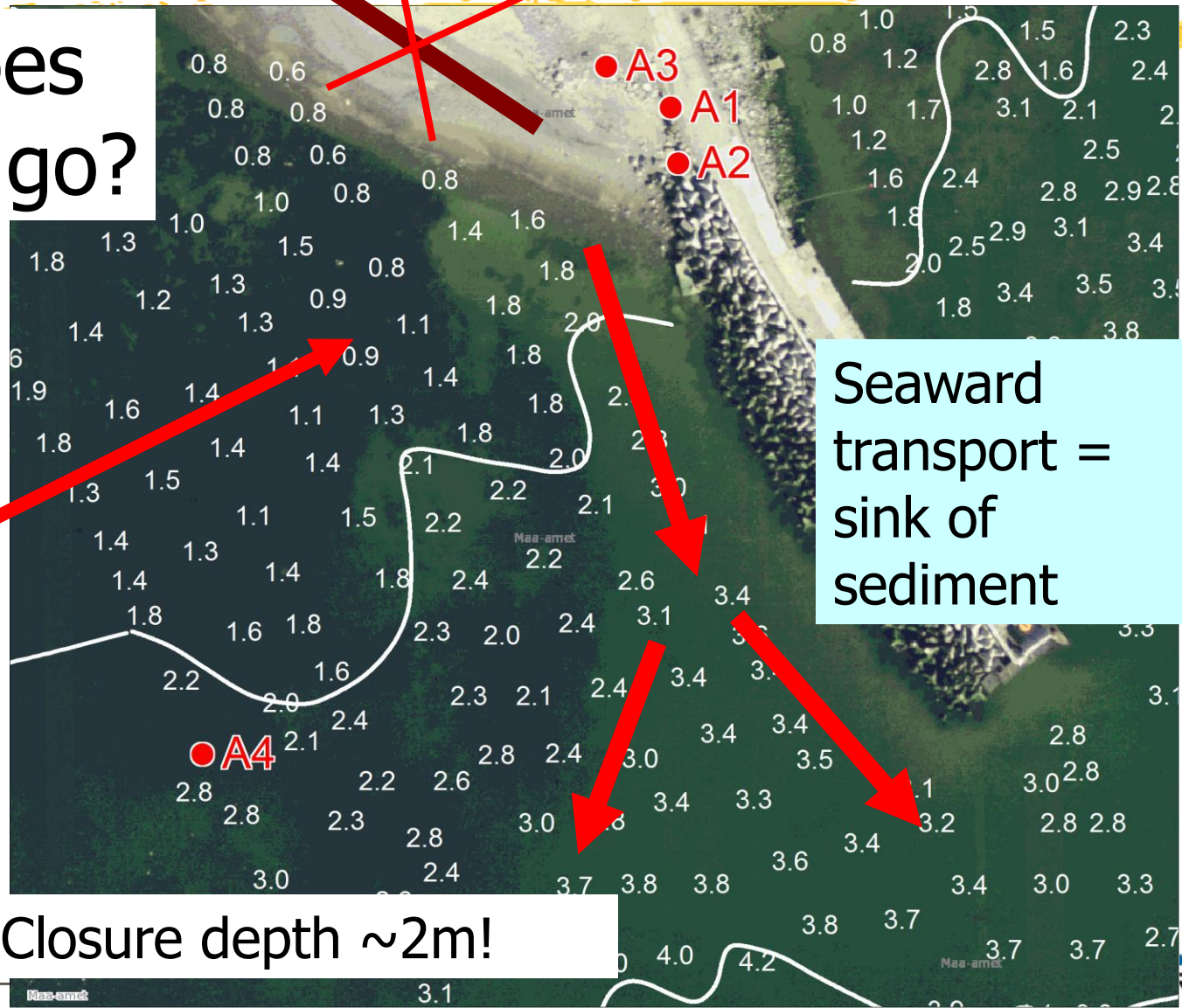




No evidence of westwards
transport

Where does
sediment go?

No fine
sediment in
this area



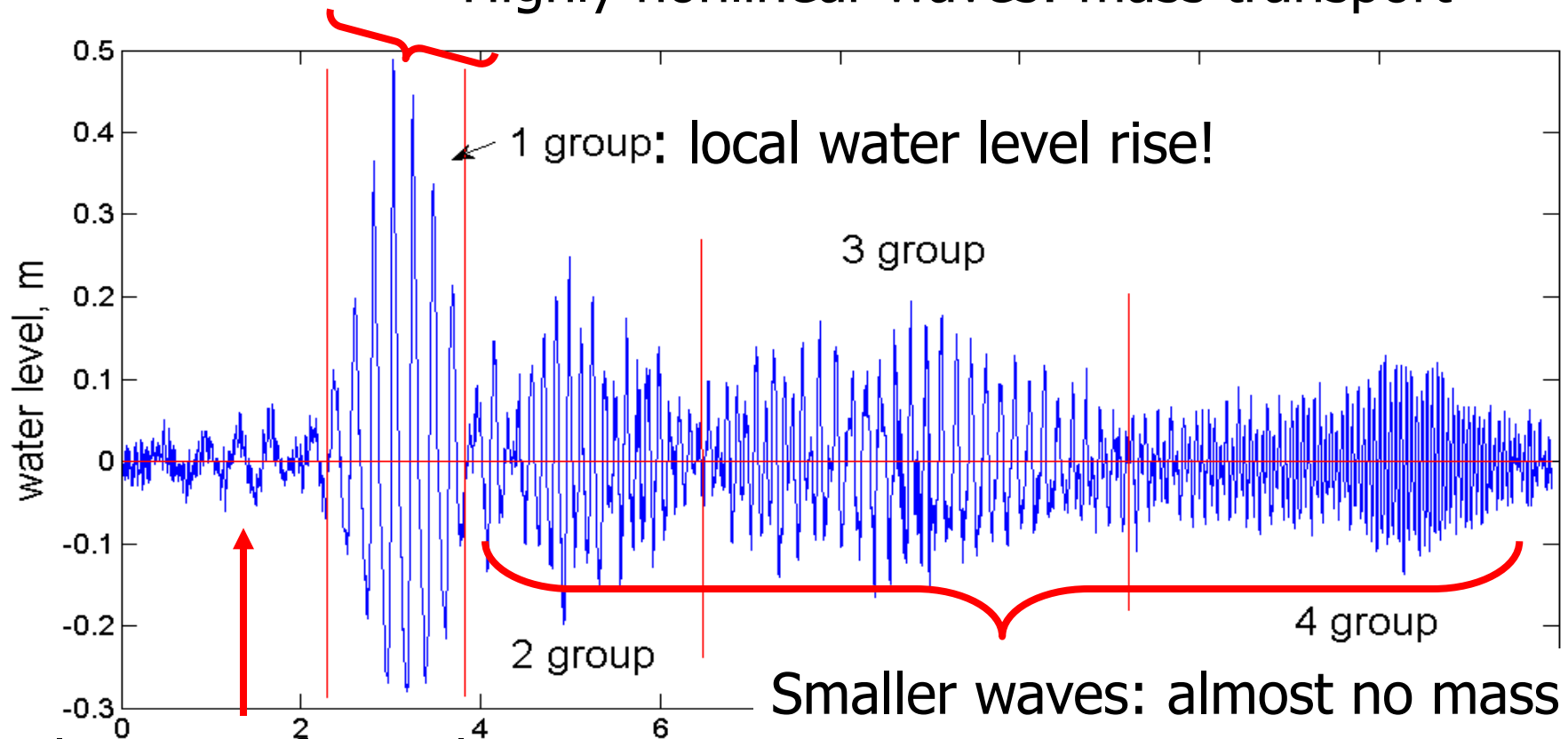
Seaward
transport =
sink of
sediment

NB! Closure depth ~2m!



Possible reason: group structure

Highly nonlinear waves: mass transport



Almost perfect solitons
carry water with them

Smaller waves: almost no mass
transport; oscillations superposed
with a strong backflow



Why intense transport seawards? (a speculation)

- Group structure of the wakes
 - ensemble of high & long waves concentrated into 1-2 minutes
- Precursor solitons and high, nonlinear leading waves
 - carry a lot of water to the coast ($\sim 10 \text{ m}^3/\text{m}$)
 - create local short-term wave setup
- followed by strong backwash
 - superposed by oscillations created by the “tail” of the wake



A selection of lessons (1)

Crossing shallow-water waves:

- up to 4-fold amplification of wave height
- up to **8-fold slope amplification**
- change of orientation of wave crests $\Rightarrow$ side hits for ships?
- easily created by topographic refraction
- may be created by temporary (ebb) jets



A selection of lessons (2)

- Ship wakes may have extremely strong impact on almost equilibrium beaches
- Large & rapid effects possible at medium-energy coasts (ship wakes: $<10\%$ of total wave energy)
- A new option: seaward transport of sediment, to the depths $\gg$ closure depth
- The impact:
 - most severe where ship wake field is almost unidirectional
 - mirrors effects of potential changes of wave climate
 - may become evident very rapidly



Lesson to take home

There are many ways of smart use of the existence of dynamical patterns on the sea

- (both natural and man-made)
- for detecting, understanding and mitigating changes
- for protecting valuable & vulnerable areas



People's response to environmental change in the light of Anacharsis

Some never learn
(even not from obvious failures)

(clear majority)

Some learn from the past

(quite few smart people)

Some face the challenge to
foresee and cope with the
changes

A "must" for the wave
& coastal community

Wishing nice & friendly sea
to everybody!

