

Let the magnetic field be directed along the  $z$ -axis. Then, when the magnetic field is being changed  $v_z = Const.$  (because  $t \gg \tau$ ). The change of the magnetic field changes the  $x-y$ -directional component. In the  $x-y$  plane, an electron with speed  $v_{xy}$  has a radius of  $R = \frac{mv_{xy}}{eB}$ . The force acting on the electron due to changing magnetic field can be expressed using the change of flux through the circular orbit of the electron. Then

$$F = -eE = -e \frac{\varepsilon}{2\pi R} = \frac{e}{2\pi R} \frac{d\Phi}{dt} = \frac{e}{2\pi R} \frac{\pi R^2 dB}{dt} = \frac{eR}{2} \frac{dB}{dt} = \frac{mv_{xy}}{2B} \frac{dB}{dt}$$

$$m \frac{dv_{xy}}{dt} = \frac{mv_{xy}}{2B} \frac{dB}{dt}$$

$$\frac{dv_{xy}}{v_{xy}} = \frac{1}{2} \frac{dB}{B}$$

$$d(\ln v_{xy}) = \frac{1}{2} d(\ln B)$$

Thus

$$\frac{v_{xy}^2}{B} = Const.$$

The change of velocity after changing the magnetic field from  $B = B_0$  to  $B = 2B_0$  is

$$\frac{v_{xy}'^2}{2B_0} = \frac{v_{xy}^2}{B_0}$$

$$v_{xy}' = \sqrt{2}v_{xy}$$

Similarly, the change of velocity by changing the magnetic field from  $B = 2B_0$  to  $B = B_0$  is  $v_{xy}' = \frac{1}{\sqrt{2}}v_{xy}$ . Initially, let the average speed of electrons be  $v_{tot0} = v_0$ . Then  $v_{tot0} = (v_z, v_{xy}) = \left(\frac{1}{\sqrt{3}}v_0, \sqrt{\frac{2}{3}}v_0\right)$ . After changing the magnetic field from  $B = B_0$  to  $B = 2B_0$ , the new velocity is  $v_{tot1} = (v_z, v_{xy}) = \left(\frac{1}{\sqrt{3}}v_0, \frac{2}{\sqrt{3}}v_0\right) = \sqrt{\frac{5}{3}}v_0$ . After time  $\mathcal{T}$ , the  $z$ - and  $x-y$ -directional velocities have stabilized and the velocity is  $v_{tot2} = (v_z, v_{xy}) = \left(\sqrt{\frac{5}{9}}v_0, \sqrt{\frac{10}{9}}v_0\right) = \sqrt{\frac{5}{3}}v_0$ . Finally, after decreasing the magnetic field from  $B = 2B_0$  to  $B = B_0$ , the total velocity becomes  $v_{tot3} = (v_z, v_{xy}) = \left(\sqrt{\frac{5}{9}}v_0, \sqrt{\frac{5}{9}}v_0\right) = \sqrt{\frac{10}{9}}v_0$ . Since  $T \propto v_{tot}^2$ , the final temperature is  $T' = \frac{10}{9}T$