Physics Cup 2017 - Problem 2 (contributed by Ivan Erofeev) without hints. 16th April 2017

There are n points forming n-gon. Adjacent points (sides of n-gon) are connected with resistance $R_s=2\,\Omega$, all other pairs (diagonals) are connected with resistance $R_s=1\,\Omega$ Find the full resistance between two adjacent points. Using your expression, calculate answer (as a rational number in ohms) for n=3, n=4, and n=5. Feel free to use mathematics software to ease algebraic calculations, if needed (such as Wolfram Alpha).