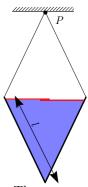
Physics Cup 2018 - Problem 4. April 8, 2018

A V-shaped vessel is made from two plates of width l and length $L\gg l$ which are connected via a frictionless hinge at its bottom. The vessel is fixed to a ceiling using light ropes of length l as shown in figure. The vessel is filled almost up to the rim with water of density ρ , and is subject to the homogeneous gravity field g. The top surface of the water is covered with a weightless thin telescopic plate which cannot be bent, but can be freely extended, and its edges can move frictionlessly up and down along the surfaces of



the inclined plates (denoted with a red line in the figure). The purpose of this telescopic plate is to keep the top surface flat during oscillations. The mass of the ropes and plates is negligible. Find the angle between the plates, and the circular frequency of the lowest-frequency mirror-symmetric oscillation mode of this system (evaluate the numerical prefactor of your expression with the precision of four significant digits). Neglect any water motion perpendicular to the plane of the figure.

First hint, 1st April. In order to understand how water moves during small oscillations, imagine drawing a set of equispaced horisontal lines onto the water. Beneath each line, there is a triangular region filled with water. As the plates move, the shapes of these triangles change, but lines remain horisontal and equispaced. Using this approach one can figure out, how the velocity of the water particles depends on the coordinates.

Second hint, April 8, 2018. Apply generalized coordinate approach: express kinetic and potential energies as a function of a small change of the angle between the plates, and of the time derivative of it (other coordinates can be used, as well; these energies can be obtained by integration over the volume of the water). Method is described, for instance, in http://www.

ipho 2012.ee/physics-solvers-mosaic/3-force-diagrams-or-general and the solvers-mosaic force-diagrams-or-general and the solvers-mosa

Correct solutions submitted during the first three weeks:

name	school	country	pr 3 solved
Dylan Toh	NUS High School	Singapore	29. Mar 18:52
T biás Marozsák	Óbudai Árpád Gimnázium	Hungary	1. Apr 17:21
Navneel Singhal	ALLEN Kota	India	2. Apr 12:57