

Physics Cup – TalTech 2019 – Problem 5. May 5, 2019

Consider a check-board-like reflective diffraction grating a cross-section of which is shown in the figure below. The height of the reflecting surface above a reference plane is given by

$$z = 20\lambda_0 \left\lfloor \frac{x}{20\lambda_0} \right\rfloor + \lambda_0 \left\lfloor \frac{y}{20\lambda_0} \right\rfloor,$$

where $\lambda_0 = 500$ nm, $\lfloor a \rfloor$ denotes the floor function (real number a is rounded down to the nearest integer), and $|x|, |y| < 5000\lambda_0$ (thus, the size of the grating is 5 mm \times 5 mm). The side surfaces (vertical edges in the figure below) of the “stairs” are black and absorb all the incident light. A parallel beam of white light containing all the wavelengths from $\lambda_1 = 400$ nm to $\lambda_2 = 700$ nm propagates parallel to the z -axis and falls onto the grating. The reflected beam is focused with a lens onto a screen perpendicular to the beam at $z = 50$ cm. Sketch qualitatively the pattern which can be seen on the screen and show the approximate dimensions of the pattern. For each wavelength, mark only the main diffraction maximum (the brightest spot). Your answer should be a set of points at $x - y$ plane (at $z = 50$ cm) showing the brightly illuminated region on the screen.



There will be no hints on 21st April. The first hints will be published on 28th April. The score for this problem is split into two parts: a sketch which captures the most important features of what can be on the screen will give a score of 0.5, and a fully correct sketch - the remaining 0.5 pts. The speed bonus will be applied separately to the both sub-scores, the penalties for submitting wrong solutions will be applied to the total score which is the sum of the two sub-scores.

By the end of the first week of the fifth problem, there were 405 registered participants from 55 countries; among them there were 204 high school students, and 201 university students. During the first week, in total 13 solutions of the fifth problem were submitted, out of which 2 were correct, and 2 more qualify as the ones capturing the most important features.

Correct solutions submitted by 21st April 2019:

Solutions capturing the most important features of the pattern which can be seen on the screen (but possibly incorrect in details).

Name	country	Uni/PreUni	subm. date/time (GMT)
Thomas Foster	UK	Oxford	14 Apr. 2019 17:22
Johanes Suhardjo	Indonesia	HKUST	14 Apr. 2019 18:34
Oliver Lindström	Sweden	PreUni	16 Apr. 2019 10:19
Oliwier Urbański	Poland	PreUni	17 Apr. 2019 10:35

Fully correct solutions.

Name	country	Uni/PreUni	subm. date/time (GMT)
Oliver Lindström	Sweden	PreUni	16 Apr. 2019 10:19
Johanes Suhardjo	Indonesia	HKUST	20 Apr. 2019 14:27